التجربة الثانية لعام 2012 - 2013		الشهادة المتوسطة	ليسه دي ژار	
الرقم :	الإسم :	المدّة : ساعتين	مسابقة في الرياضيات الانكليزي	

إرشادات عامة:

- يسمح بإستعمال ألة حاسبة غير قابلة للبرمجة
- يمكن الإجابة على ألمسائل بالترتيب الذي تريد
 - يرجى الإجابة بخط واضح ومرتب
 - العلامة القصوى من 40
 - عدد المسائل: 5

<u>1st exercise: (7½pts)</u>

In this exercise, the four parts are independent.

1) Consider the following equation (E): $\frac{4^4 - 2^3}{2^3} = 2^{2n+1} - 1$.

Calculate the value of the <u>unknown n</u>. (1½pts)

2) In the plane referred to an orthonormal system of axes x'ox, y'oy, consider the points A(1, -1), B(3, 3) and C(1, 7).

We admit without proof that triangle ABC is isosceles at B.

Determine an equation of the internal bisector of angle ABC. (1 ½ pts)

- 3) Consider a rectangle of perimeter 20m and length $\,\ell$.
 - a) Express the area A in terms of ℓ . Can you say that A is a linear function of ℓ ? Explain. (1½pts)
 - b) Show that $A = 25 (\ell 5)^2$. (¹/₂ pt)
 - c) Deduce the value of ℓ for which the **area is maximum**. (1pt)
- 4) The area of a room is $20 m^2$. The decorator offered a 5% discount for the tiling (تبليط) so that the total price of tiling for the room after discount is 4275\$. Calculate the price of each m^2 of tiling before the discount. (1 ½ pts)

2nd exercise: (41/2pts)

ABCD is a rectangle such that AB = 6cm and BC = 4cm.

M and N are two points of [AB] and [CD] respectively such that AM = CN = x.

- 1) Write an encirclement for $\underline{\mathbf{x}}$. (¹/₂ pt)
- 2) a) Calculate the area A_1 of triangle CBM then deduce the area A_2 of the parallelogram AMCN. (1 ¹/₂ pts)
 - b) What type of functions are A_1 and A_2 ? Justify. (1pt)
- 3) Determine <u>x</u> so that the area of the parallelogram AMCN is **the double** of ← that of the **shaded part**. (1¹/₂pts)

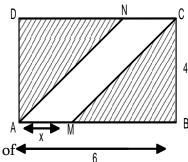
3rd exercise: (12 pts)

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In an orthonormal system x'ox, y'oy, consider the points A(2,-2), B(-1, 2) and C(6, 1). $M\left(\frac{5}{2}, m\right)$ is a

variable point where m is a real parameter and (d) is the straight-line of equation $y = \frac{3}{4}x - \frac{7}{2}$.

- 1) Plot the points A, B and C. (1pt)
- 2) Show that (d) passes through the points A and C then draw (d). (1¹/₄pts)
- 3) a) Determine the set of points M as m varies. (1 pt)
 - b) Calculate $a_{(BC)}$, the slope of (BC) and verify that $a_{(AM)} = 2m + 4$. (1½pts)



c) Determine m so that the two straight-lines (BC) and (AM) are perpendicular. (1pt)

<u>In what follows, take</u> $m = \frac{3}{2}$ so that $M\left(\frac{5}{2}, \frac{3}{2}\right)$

4) a) Show that M is the midpoint of [BC]. (³/₄ pt)

b) Calculate the lengths BC and AM then verify that $AM = \frac{BC}{2}$. (1 ¹/₂ pts)

c) Deduce the nature of triangle ABC. (1pt)

- 5) Let (Δ) be the straight-line perpendicular to (AC) and passing through the point K(3, 4).
 - a) Determine the equation of (Δ) . (1pt)
 - b) Verify that the point S(9,-4) is the point of intersection between (Δ) and the straight-line (L) having an ordinate of the origin 2 and an x-intercept 3. (2pts)

4th exercise: (81/2pts)

The manager of a theatre proposes two options to his spectators:

<u>Option 1</u>: Pay a sum of 60 € per session.

- **Option 2:** Pay an annual subscription of 210 € and obtain a discount of 25% on each session that costs 60 €.
- 1) What is the advantageous option if the spectator wants to attend 15 sessions in one year? Justify.(1¹/₂pts)
- 2) Designate by x the number of sessions attended in one year.
 - f(x) is the sum paid in \in in option 1.
 - g(x) is the sum paid in \in in option 2.
 - a) Express f(x) in terms of x then show that g(x) = 45x + 210. (1 ¹/₂ pts)
 - b) Complete the following table and show your work: (1 ¹/₂ pts)

Х	0	2	14
f(x)			
g(x)			

c) Represent graphically the two straight-lines (d_1) and (d_2) representing the two functions f and g respectively.

Note: the plane is referred to an orthogonal system where:

- On the x-axis, 2cm corresponds to 1 session.
- On the y-axis, 1 cm corresponds to 50 €. (1 ½ pts)
- 3) a) Solve the equation f(x) = g(x) and interpret the obtained result. (1pt)
 - b) Discuss graphically, according to the values of x, the most advantageous option for the spectator. (1 ½ pts)

5th exercise: (7 ½ pts)

Consider the circle (C) of center O and diameter AC = 10cm. D is the point of (C) such that $\overrightarrow{CD} = 60^{\circ}$. Let I be the orthogonal projection of D on [AC]. (DI) cuts the circle in E and <u>the two straight-lines (AD) and</u> (EC) meet at F.

- 1) Draw a figure in true measures. (1pt)
- 2) Show that (DO) and (FC) are parallel then deduce that D is the midpoint of [AF]. (1 ½ pts)
- 3) Calculate the lengths FC, FA and AI. (2pts)
- 4) In this part, consider that D is a variable point on (C), and M is the midpoint of [AD].
 - a) What does (OM) represent for [AD]? Justify. (1pt)
 - b) Deduce the locus of M as D varies on (C). (1pt)
 - c) Let G be the centroid of triangle ADC. Determine the locus of G. (1pt)