

I- A 9th-grade teacher **collects** the grades of his students in Arabic test per 30.

29 ; 12 ; 20 ; 22 ; 28 ; 15 ; 30 ; 25
24 ; 13 ; 25 ; 17 ; 23 ; 19 ; 29 ; 28
20 ; 19 ; 17 ; 21 ; 15 ; 21 ; 15 ; 23

- 1) How can you describe the **organization** of the above data?
 - a) Ordered
 - b) Random
 - c) Simple
- 2) Which **objects** (people, animals ...) are **under study**?
.....
- 3) What is the **aspect** that is being **studied**?
.....
- 4) What is the **number** of **subjects** under study?
.....
- 5) What is the highest mark collected?
- 6) Which is the most frequent mark?
- 7) How many students took 15?

II- A 9th-grade teacher **collects** the grades of his students in a math test per 30 and organize them in the following way:

Grades	12	13	15	17	20	22	25	28
Number of students	1	2	2	1	4	5	3	7

- 1) How can you describe the **organization** of the above data?
 - a) Ordered
 - b) Random
 - c) Simple
- 2) Which **objects** (people, animals ...) are **under study**?
.....
- 3) What is the **aspect** that is being **studied**?
.....
- 4) What is the **number** of **subjects** under study?
.....
- 5) What is the highest mark collected?
- 6) Which is the most frequent mark?
- 7) How many students took 15?

Conclusions:

- a) Which of the above ways of collecting data was more readable?
- b) If the second way is called the statistical way, then
 - i. What does statistics do?
 - ii. How is it useful?
 - iii. Where would you think that we can use statistics?

✓ **Introduction:** Statistics which is a synonym for “numerical facts” is a relatively new branch of mathematics that aims at:

- 1) Collect data.
- 2) Classifying, summarizing and organizing data.
- 3) Reading data in a more efficient way.
- 4) Representing data in different forms (pie graph, histogram, bar graph ...).
- 5) Interpret and find relation among data.
- 6) Draw out conclusions from a given set of data.

✓ **Usages:** almost every field of studies benefit from organizing statistical surveys.

👁️ **Educational field:** Teachers evaluating students over a specified set of objectives (factorize, develop, graph, conduct a geometric proof...).

👁️ **Entertainment:** A TV show analyzing a football match (goals scored, shoots on target percentage of ball possession...)

👁️ **Industry:** A company introducing a new product to the market (study of profit per month)

✓ **Statistical vocabulary:**

- **Population:** is the set of observed elements having a common property.

- The set of students in a class.
- The set of teams in a certain league.

- **Size:** is the total number of elements in a population.

- **Character (values, variable) (x_i):** is the common property of the population under study.

- The height, weight, grades.... of an individual in a set of population.
- The color of eyes, gender (male, female), behavior of an individual in a population.

▪ Types of characters:

1) **Quantitative:** a character is said to be quantitative if it can be measured.

✓ Length, number of children, number of books read

2) **Qualitative:** a character is said to be qualitative if it cannot be measured.

✓ The color of eyes, gender (male, female), behavior, scent, taste, shapes....

- **Frequency(n_i):** is the number of times a character is observed.

👁️ **Note that:** The total frequency or size is the sum of all frequencies and it is denoted by N.

- **Relative frequency($R.f$):** is the ratio of the frequency(n) to the size (N) of an object.

$$\text{In symbols: } R.f = \frac{n}{N}$$

👁️ **Note that:** The relative frequency is a number strictly included between 0 and 1

$$\text{In symbols: } 0 < R.f < 1$$

✓ **Measure of central tendency:**

- **Range(R):** is the difference between the highest and lowest observed values for a quantitative character.
- **Mode:** is the variable that admits the highest frequency.
 - Having two modes is called "**bimodal**".
 - Having more than two modes is called "**multimodal**".
- **Mean (Average):** is of two main types
 - **Arithmetic Mean:**
Def: is the ratio of the sum of values to the size of the population.
Formula: $\bar{X} = \frac{\sum x_i}{N}$
 - **Weighted mean:**
Def: is the ratio of the sum of product of values by their frequencies to the size.
Formula: $\bar{X} = \frac{\sum x_i \cdot n_i}{N}$

✓ **Cumulative frequency:**

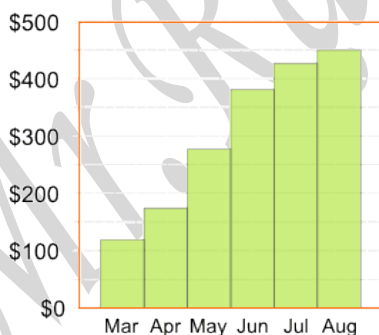
- Cumulative means "how much so far".

Think of the word "accumulate" which means to gather together.

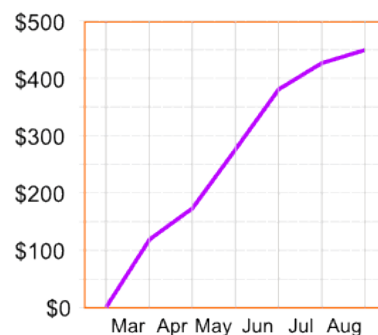
- Types of cumulative frequencies:

➤ **Increasing cumulative frequency (ICf)**

You can make cumulative graphs if you want.



Increasing Cumulative Histogram



Increasing Cumulative Line Graph

➤ **Decreasing cumulative frequency (DCf)**

To have cumulative totals, just **add up the values as you go.**

Histograms vs Bar Graphs

Bar Graphs are good when your data is in **categories** (such as "Comedy", "Drama", etc). But when you have continuous data (such as a person's height) then use a Histogram. It is best to leave gaps between the bars of a Bar Graph, so it doesn't look like a Histogram

👁️ Using a calculator:

🌀 How can we use the calculator to find some statistical indicators?

CASIO <i>fx-991ES</i>	CASIO <i>fx-991ES</i>
1- Mode2 2- Shift/clr/1/=	1- Mode/3/stat/1:1-var 2- On
3- Enter data: i) Variable/shift/,/frequency/m+	3- Shift/mode 4- Down
4- To find: a) Mean: press shift/2/1/=	5- 4:stat/1:on 6- Same as step 1.
b) Standard deviation: press shift/2/2/=	7- Fill data. 8- Ac
	9- Shift/1 10- Press: 4: var
	Choose one you want to cal. i. Mean: \bar{x} ii. Standard deviation.

Project

Choose one of the following surveys, and then answer the related questions given at the end

S-1: Study the distribution of tourists among five Lebanese cities.

S-2: Study the number of goals scored in the last ten games for your best five football teams.

S-3: Study the number of points scored by five players in a basketball match between your two favorite teams.

S-4: Study the number of hours you spend preparing for each of five of your school assignments.

For each statistical survey specify (on your own):

- 1) The population and the size of the chosen sample space.
- 2) The variable under study (character) and its type (Qualitative or Quantitative)
- 3) The range of the data if possible.
- 4) The highest and the lowest values among the specified data.
- 5) The average (mean) of your data.