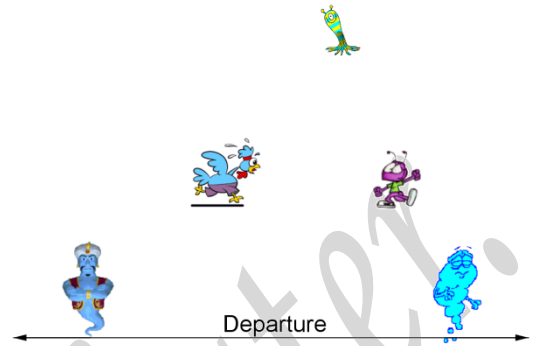


Focusing event:

A race is on hold between a chicken and an ant where the alien is the referee. If the genee and the gohst are 10m apart, and both compatetors are midway between the departure line and the referee. Can you find how far is the chicken from the ant?



**Midpoint theorem in a triangle**

I- Let  $M$  &  $N$  be the respective midpoints of sides  $[AB]$  &  $[AC]$  in triangle  $ABC$ .

1. Draw a clear figure.
2. Plot  $K$  the symmetric of  $M$  with respect to  $N$ .
  - a. Determine the nature of the quadrilateral  $AKCM$  ? Justify.



.....  
 .....  
 .....

b. Prove that  $MKCB$  is a parallelogram.

.....  
 .....

3. Deduce that:
  - a.  $BC = 2MN$  : .....
  - b.  $(MN)$  parallel  $(BC)$  : .....

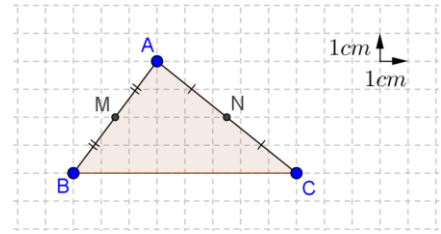
<b>Conclusion:</b>	<ul style="list-style-type: none"> <li>✓ The segment joining the midpoints of two sides of a triangle is .....</li> <li>✓ The straight line joining the midpoints of two sides of a triangle is .....</li> </ul> <p>The above statements are the midpoint theorem in any triangle.</p>
--------------------	--

<b>Conditions and usage:</b>	<ul style="list-style-type: none"> <li>✓ Conditions: To use midpoint theorem we should have:                      ☞ .....</li> <li>✓ Usage: We use the midpoint theorem to:                      ☞ .....                      ☞ .....</li> </ul>
------------------------------	--



Application: Consider the triangle  $ABC$  :

1) What do the points  $M$  &  $N$  represent?



2) Determine:

a.  $[AB]$  in terms of  $[AM]$  : .....

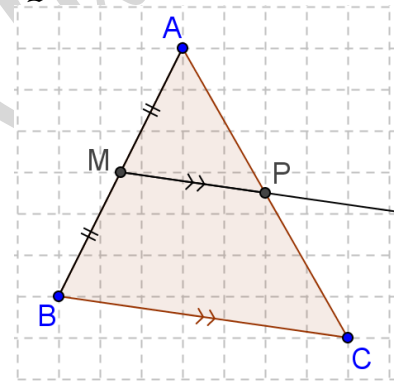
b.  $[AN]$  as a function of  $[AC]$  : .....

3) Find the ratio of  $[MN]$  to  $[BC]$ .

### Converse of midpoint theorem in a triangle

**II-** In the adjacent figure  $M$  is the midpoint of  $[AB]$  and  $[MP]$  is parallel to  $(BC)$ .

Devise a method to prove that  $P$  is the midpoint of  $[AC]$ .



### Conclusion:

✓ If a line is issued from the midpoint of a side of a triangle and parallel to the second side, then it must cut the third side at .....

### Conditions and usage:

✓ Conditions: To use converse of midpoint theorem we should have:

☞ .....

☞ .....

✓ Usage: We use the converse of midpoint theorem to:

☞ .....

