Sets of numbers: numbers are classified into sets (groups) according to their purpose.

1. Natural numbers:

When you are counting the number of pages of a book or any other thing we use: $0,1,2,3,4,5,\ldots$ etc.

The set of natural numbers is denoted by: $\mathbb{N} = \{0, 1, 2, 3, 4, 5, ...\}$

<u>*Ex₁*</u>: Solve the following equations in \mathbb{N} and what do you notice: x+3=5

2. Integers:

As you noticed, from the above example that some equations of the form x+a=b, where a & b belong to \mathbb{N} cannot be solved in the set \mathbb{N} . So we will extend the set \mathbb{N} to the set of integers \mathbb{Z} , which stands for **Zahlen** and consists of the set \mathbb{N} and its opposite.

<u>In other words</u>: $\mathbb{Z} = \{\dots -3, -2, -1, 0, 1, 2, 3...\}$.

$$\succ Notice that: \mathbb{N} \subset \mathbb{Z}$$

<u>*Ex*</u>₂: Solve the following equations in \mathbb{Z} : $x^2 - 4 = 0$, 2x + 3 = 0.

3. <u>Rational numbers</u>:

 \mathbb{Z} , is insufficient to solve some equations of the form ax + b = 0, where a & b belong to \mathbb{Z} .

So, we will extend the set \mathbb{Z} into the set of *rational* numbers.

The word rational is derived from ratio. So, we can deduce that any number that can be written in the ratio form, $\frac{a}{b}$, where a & b are integers such that $b \neq 0$ is said to be a rational number.

The set of rational numbers includes numbers of the form:

$$\mathbb{Q} = \left\{ \dots, -\frac{1}{3}, -\frac{1}{2}, -\frac{1}{1}, 0, \frac{1}{3}, \frac{1}{2}, \frac{1}{1}, \dots \right\}$$
$$\mathbb{Q} = \left\{ x \mid x = \frac{a}{b}, \forall a \in Z \& b \in Z^* \right\} In comprehension.$$

 \succ Notice that: : $\mathbb{Z} \subset \mathbb{Q}$

10th Grade.

Mathematics E.S.2. Sets of Numbers

4. Irrational numbers:

Are numbers that *can't* be written in the form of a ratio, $\frac{a}{b}$ where a & b belong to \mathbb{Z} and $b \neq 0$.

Common forms of irrational numbers:

$$\approx \sqrt{2}, \sqrt{3}, \sqrt{5}, \sqrt{6}...$$

 $\approx \pi \approx 3.1415...$
 \approx Numbers, in decimal form with infinite non periodic decimal part. *E.g*: 7.9425721...

How to represent an irrational number on a number line?

To represent a number of the form: \sqrt{a}

- 1- Square the given number to get a.
- 2- Place on y axis a point A so that OA = a cm.
- 3- Always place on y axis from below a point B so that OB = 1cm.
- 4- Trace a circle whose diameter is [AB].
- 5- The intersection of the circle with the $\oplus vex axis$ is the position of \sqrt{a}

5. <u>Real numbers</u>:

Is the set of all numbers, it includes all of the above sets, \mathbb{N} , \mathbb{Z} , \mathbb{Q} and the set of irrational numbers.

This set includes numbers of the form: $\Re = \left\{ ..., -2, -\frac{1}{2}, 0, 1, \sqrt{2}, \pi, 4.5... \right\}$

Conclusion:
$$\mathbb{N} \subset \mathbb{Z} \subset \mathbb{Q} \subset \mathfrak{R}$$

<u>32 ote that</u>:

J- If a set of numbers is raised to the symbol "*" "star" then this means that it is the same set except we exclude from it zero.

$$N^* = \{1, 2, 3, 4, \dots$$

 $N^* = N - \{0\}$

If a set of numbers is raised to the symbol "+" "plus" then this means that it includes only the positive part of the set.

$$Z^{+} = \{0, 1, 2, 3, ...\}$$
$$Z^{+} = \{x \mid x \in N, \forall x \ge 0\}$$

JJJ - If a set of numbers is raised to the symbol "-" "minus" then this means that it includes only the negative part of the set.

$$Z^{-} = \{..., -3, -2, -1, 0\}$$

$$Z^{-} = \{ x \mid x \in Z, \forall x \le 0 \}$$

10th Grade.

Mathematics E.S.2. Sets of Numbers



 $\sqrt{3}$

Summary of the lesson using:

