Lycée Des Arts Name:

Mathematics "All about Remarkable lines"

I- <u>Remarkable lines</u>:

Line	Definition	Graph	How to draw?
Median	is a semi straight line issued from the vertex of a triangle and cuts the opposite side at its midpoint	Height	Height
Altitude (height)	is a semi straight line issued from the vertex of a triangle and is perpendicular to the opposite side	Median	Median
Bisector	is a semi straight line issued from the vertex of a triangle and cuts the included angles into two equal adjacent parts.	Bisector	Bisector
Perpendicular bisector	is a straight line that is perpendicular to a segment at its midpoint		

a. Property of an angular bisector:



b. Property of a perpendicular bisector:

<u>Conclusion</u>: Any point on the perpendicular bisector of a segment is equidistant from its extremities.



II- <u>Remarkable points in a triangle:</u>

a- Center of gravity or centroid: is the intersection of medians in a triang	gle.
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Properties	Geometric figure	Uses
The centroid divides each median in the ratio $\frac{2}{3}$ starting from the vertex <i>That is</i> ; $AG = (2/3) AA'$ A'G = (1/3) AA' AG = 2 A'G	B A'I C	<i>Center of mass</i> is a point at which the mass of an object is concentrated.

- *b- Orthocenter*: is the intersection point of the altitudes in a triangle.
- *c- Circumcenter or center of the circumscribed circle*: is the intersection point of the perpendicular bisector.
 - ✓ <u>Uses</u>: The *circumcenter* is a point at which we can plot the center of the circle that passes through the three vertices of a given triangle.



- *d- Incenter or the center of the inscribed circle*: is the intersection point of the bisectors of the angles in a triangle.
 - ✓ <u>Uses</u>: The *incenter* is a point at which we can plot the center of the circle that remains tangent to all three sides of the given triangle.

