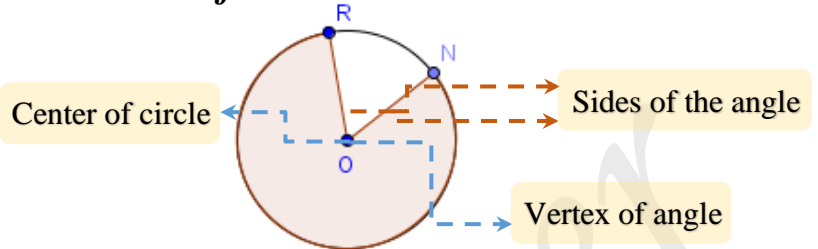


Name:

ξ **Central angle:**

Def: is an angle whose **vertex is the center of the circle** and its sides intersect the circle **at two distinct points**.

\widehat{RON} is a central angle.



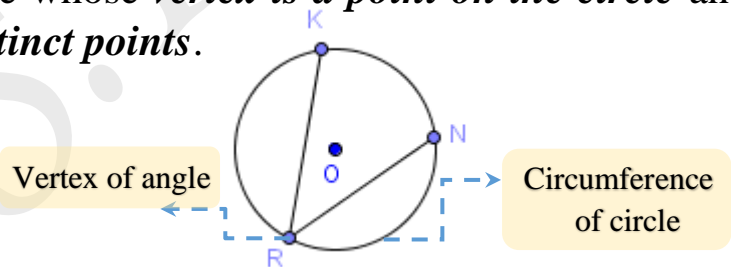
ξ Property: Measure of central angle is equal to measure of the arc it intercepts.

Graphically			
In symbols	$\widehat{AOB} = \text{mes}\widehat{AB}$	$\widehat{SOK} = \text{mes}\widehat{SK}$	$\widehat{RON} = \text{mes}\widehat{RN}$

ξ **Inscribed angle:**

Def: An **inscribed angle** is an angle whose **vertex is a point on the circle** and sides intersect the circle **in two distinct points**.

\widehat{KRN} is an inscribed angle.



ξ Property-1: Measure of inscribed angle equals half measure of intercepted arc.

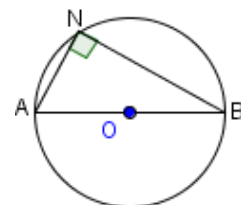
Graphically				
In symbols	$\widehat{FAE} = 25^\circ$ $\text{mes}\widehat{FE} = 50^\circ$ So, $\widehat{FAE} = \frac{1}{2}\text{mes}\widehat{FE}$	$\widehat{AEC} = 60^\circ$ $\text{mes}\widehat{AC} = 120^\circ$ So, $\widehat{AEC} = \frac{1}{2}\text{mes}\widehat{AC}$	$\widehat{AEC} = 60^\circ$ $\text{mes}\widehat{AC} = 120^\circ$ So, $\widehat{AEC} = \frac{1}{2}\text{mes}\widehat{AC}$	$\widehat{RON} = \text{mes}\widehat{RN}$

ξ Property-3: Measure of the **inscribed angle facing the diameter** is equal to 90° .

Decoding: If N is a point on (C) and [AB] is a diameter of (C).

then, $\widehat{ANB} = \frac{\widehat{AOB}}{2} = \frac{180^\circ}{2}$

Thus, $\widehat{ANB} = 90^\circ$. (Thales' 5th theorem)



ξ Types of exterior angles:

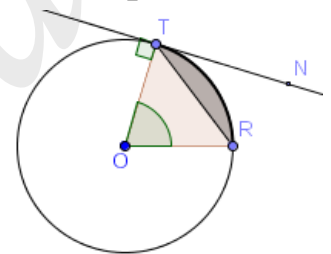
<u>Graphical form:</u>			
<u>Description:</u> Exterior angle formed between	Two secants	Two tangents	A secant & a tangent
<u>Measure:</u>	$R\hat{P}N = mes \frac{\widehat{RN} - \widehat{SK}}{2}$	$B\hat{A}C = mes \frac{\widehat{BNC} - \widehat{BC}}{2}$	$R\hat{K}N = mes \frac{\widehat{RN} - \widehat{MN}}{2}$
<u>In words:</u>	Angle between 2 secants	Angle between two tangents	Angle between a tangent & a secant
	issued from an exterior point equals half the difference of the two intercepted arcs.		

ξ Angle between tangent and chord:

Def₃: is an angle issued from the point of tangency and it is equal to half the intercepted arc.

Decoding: If [TN] is a tangent to (c) at T. and [TR] is a chord of (c)

$$\text{Then, } R\hat{T}N = mes \frac{\widehat{TR}}{2}$$



ξ Interior angle: Angle enclosed between **two chords intersecting inside the circle** equals half the sum of the two intercepted arcs.

Proof: In triangle ACM we have:

$$A\hat{M}D = M\hat{A}C + A\hat{C}M \left\{ \begin{array}{l} \text{(Exterior angle equals sum of} \\ \text{opposite interior angles in a triangle} \\ \text{(flag rule) check E.S-6.)} \end{array} \right.$$

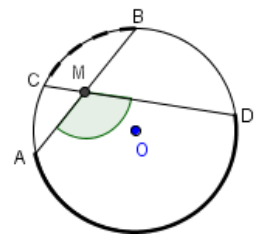
But, points A, M & B are collinear (given)

And, points C, M & D are collinear (given)

$$\text{So, } M\hat{A}C = mes \frac{\widehat{BC}}{2} \text{ (inscribed angle)}$$

$$\text{And, } A\hat{C}M = mes \frac{\widehat{AD}}{2} \text{ (inscribed angle)}$$

$$\text{Thus, } A\hat{M}D = mes \frac{\widehat{AD} + \widehat{BC}}{2}$$



Some properties of arcs and angles

<u>Property</u>	<i>Description</i>	<i>If</i>	<i>Then</i>	<i>Graph</i>
1	Arcs included between parallel chords in a circle are equal .	$[PE] \parallel [RF]$	$\widehat{PR} = \widehat{EF}$	
2	Inscribed angles intercepting the same arc are equal	$B\widehat{E}C$ And $B\widehat{D}C$ intercepts same arc \widehat{BC}	$B\widehat{E}C = B\widehat{D}C$ $= \text{mes } \frac{\widehat{BC}}{2}$	
3	Equal chords subtend equal arcs .	Chords KN & IR are equal	Then, $\widehat{KN} = \widehat{IR}$	
4	Equal arcs subtend equal chords	$\widehat{KN} = \widehat{IR}$	Then, Chords KN & IR are equal	
5	Equal angles intercept equal arcs and vice versa	If, $E\widehat{F}G = A\widehat{B}C$.	Then, $\widehat{EG} = \widehat{AC}$	
6	Chords equidistant from the center of the circle are equal .	If $OH = OK$	Then, chords AB & CD are equal	
7	Equal chords are equidistant from the center .	If, Chords QP & RS are equal	Then, $OH = OK$ Or O is equidistant from points H & K	

☛ Rule-1:

(Perimeter of a circle): $2\pi R \longrightarrow 360^\circ$ (*Greatest angle in a circle*)

(Length of an arc): $L \longrightarrow R\hat{O}N$ (*Central angle corresponding to L*)

$$\text{Length of an arc} = \frac{2\pi R \times R\hat{O}N}{360^\circ}$$

☛ ☛ Rule-2:

(Area of a circle): $\pi R^2 \longrightarrow 360^\circ$ (*Greatest angle in a circle*)

(Area of a circular sector): $A \longrightarrow R\hat{O}N$ (*Central angle corresponding to A*)

$$\text{Area of a circular sector} = \frac{\pi R^2 \times R\hat{O}N}{360^\circ}$$