## Lycée Des Arts

Name / Nom : $\qquad$
$\square$
Class / Classe : Grade 8 Section: ....... Date

## Exam in / Examen de: Math

## Exercise 1:(11 pts)

In the following table, only one of the proposed answers is correct. Indicate it and justify your choice.

| № | Questions | Answers |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | A | B | C |
| 1 | In the following figure we have : <br> $A B C D$ is a square of side 6 cm . <br> $M$ and $N$ are two points on $[A B]$ and $[A D]$ respectively such that: $M B=D N=4 \mathrm{~cm}$ <br> The area of the shaded part represents the..................(2½ pts) | $\frac{1}{3}$ of the area of the square | $\frac{1}{4}$ of the area of the square | $\frac{1}{5}$ of the area of the square |
| 2 | If $\boldsymbol{A}=\left(\frac{4}{3}\right)^{-1}-\frac{3+\frac{5}{4}}{5-\frac{1}{7}}$ <br> and $\boldsymbol{B}=\frac{96 \times 10^{-6} \times(-5) \times 10^{-1}}{2^{-6} \times 3 \times 5^{-6} \times 2}$ <br> Then $A$ is ...........( 2 pts ) | The reciprocal of $B$ | The opposite of $B$ | Equal to $B$ |


| 3 | In the following figure we have : <br> - $A B C$ is a triangle and $O$ belongs to $[A C]$. <br> - $I$ is the midpoint of $[A B]$. <br> - $I O=I A=I B$. <br> - Jis the midpoint of $[B C]$. <br> Then the triangle OJC is......... (2 pts) | Isosceles <br> at J | Equilateral | Rectangle at J. |
| :---: | :---: | :---: | :---: | :---: |
| 4 | Given $F=\frac{3 x-5}{5 x-2}+\frac{16-9 x}{4-10 x}$. Then $F$ is: $\qquad$ .(11/4 pts) | A literal fraction for $x \neq \frac{2}{5}$ | A decimal fraction | Not Decimal |
| 5 | The approximate value of : $A=\frac{2+\frac{1}{3}+\frac{1}{1+\frac{1}{3}}}{1-\frac{1}{2}}$ to the nearest hundredths by excess is ..........(11/4 pts) | 6,2 | 6,16 | 6,17 |
| 6 | $(\mathrm{S})$ is a circle of center $O$ and diameter $[A B] . C$ is a point of $(S)$ and $D$ is the symmetric of $B$ with respect to $C$. The lines $(A C)$ and $(D O)$ intersect at $E$. The line ( $B E$ ) in the triangle $A B D$ is ...(2 pts) | A median | An angle bisector | A height |

## Exercise 2: ( $101 / 2 \mathrm{pts}$ )

Given the following algebraic expressions:
$G(x)=4(x-1)^{2}-(3 x+2)^{2}$ and $H(x)=(x+4)^{2}-(x+3) \cdot(x+4)+2 x^{2}-32$

1) a) Expand and reduce $H(\boldsymbol{x})$. (1pt)
b) Solve $H(\boldsymbol{x})=-28 .(1 \mathrm{pt})$
2) a) Show, by factorizing, that: $G(x)=-5 x \cdot(x+4)$ and $H(x)=(x+4) \cdot(2 \boldsymbol{x}-7) \cdot(2 \mathrm{pts})$
b) Deduce the roots of $G(x)$. $(1 \mathrm{pt})$
3) Let $S A L I$ be a parallelogram such that $S A=G(\boldsymbol{x})$ and $A L=H(\boldsymbol{x})$.
a) Does the side $[S A]$ exist for $\boldsymbol{x}=-4$ ? Justify. $(3 / 4 \mathrm{pt})$
b) Calculate the numerical value of $A L$ for $\boldsymbol{x}=1$. What do you notice? $(3 / 4 \mathrm{pt})$
c) Is there any value of $\boldsymbol{x}$ for which $S A L I$ is a rhombus? Justify. ( $1 \frac{1}{4} \mathrm{pts}$ )
4) We consider the fractional expression $R(\boldsymbol{x})$ defined by: $R(\boldsymbol{x})=\frac{\boldsymbol{G}(\boldsymbol{x})}{\boldsymbol{H}(\boldsymbol{x})}$.
a) Determine the domain of definition of $R(\boldsymbol{x})$, then simplify it.( $11 / 4 \mathrm{pts}$ )
b) Calculate $R\left(-\frac{1}{2}\right) .(1 / 2 \mathrm{pt})$
c) Is there any value of $\boldsymbol{x}$ such that $R(\boldsymbol{x})=-\frac{5}{2}$ ? Justify. (1pt)

## Exercise 3: ( $81 / 2 \mathrm{pts}$ )

Let $A B C$ be a right triangle at $A$ such that $B C=6 \mathrm{~cm}$ and $\boldsymbol{A B C}=30^{\circ} .[A H)$ is the height relative to $[B C] . A^{\prime}$ is the symmetric of $A$ with respect to $H$, and $M$ is the midpoint of $[B C]$.

1) Draw a clean figure. ( $1 / 2 \mathrm{pt}$ )
2) Prove that the triangles $A C H$ and $A^{\prime} C H$ are congruent, then deduce the measure of angle $\widehat{A^{\prime} C B} \cdot\left(1^{1 / 2} \mathrm{pts}\right)$
3) a) Calculate $A M$, then deduce that $A C M$ is an equilateral triangle.(1pt)
b) Show that $C A M A^{\prime}$ is a rhombus.(1pt)
4) Show that the triangles $A C B$ and $A^{\prime} C B$ are congruent then deduce that $[B C)$ is the angular bisector of $\widehat{A B A^{\prime}} \cdot\left(1^{1} / 2 \mathrm{pts}\right)$
5) Draw: $(1 / 2 \mathrm{pt})$
${ }^{*} H^{\prime}$ the symmetric of $H$ with respect to $A$.
${ }^{*} C^{\prime}$ the symmetric of $C$ with respect to $A$.
${ }^{*} M^{\prime}$ the symmetric of $M$ with respect to $A$.
a) Determine the nature of the quadrilateral $C H C^{\prime} H^{\prime} .(3 / 4 \mathrm{pt})$
b) Prove that $C^{\prime} H^{\prime}=1.5 \mathrm{~cm} .(1 / 2 \mathrm{pt})$
c) Prove that $C C^{\prime}=M M^{\prime}$, then deduce that the quadrilateral $C M C^{\prime} M^{\prime}$ is a rectangle.( $1 \frac{1}{4} \mathrm{pts}$ )
