

Subject: Mathematics

Class: Grade 10



Duration: 150 minutes

**Question I : (4pts)**

In the table below, only one of the proposed answers to each question is correct. Write down the letter corresponding to the proper answer, **with justification**.

n°	Questions	Answers		
		a	b	c
1	If $ x^2 - 5  = -3$ then	No solution for x	$x \in \{2\sqrt{2}, -2\sqrt{2}\}$	$x \in \{-\sqrt{2}, \sqrt{2}, 2\sqrt{2}, -2\sqrt{2}\}$
2	If $[-5, 1] \cap X = [-3, 1]$ , then $X =$	$[-3, 3[$	$] -3, +\infty [$	$] -5, -3 ]$
3	Given: $\sin x = \frac{\sqrt{3}}{3}$ . Then $\cos(x + \frac{5\pi}{2}) =$	$\frac{1}{\sqrt{3}}$	$-\frac{1}{\sqrt{3}}$	$\frac{\sqrt{2}}{3}$
4	If $x < 0$ , then $\frac{\sqrt[4]{x^4}}{\sqrt[3]{x^3}} =$	does not exist	-1	1

**Question II : (2.5 pts)**

Consider the sets:  $A = \{x \in \mathbb{Z} / (x-1)(x^2-16)(2x+1) = 0\}$  &  $B = \{x \in \mathbb{IN} / |x - \frac{3}{2}| < \frac{5}{2}\}$

- 1) Show that :  $A = \{-4, 1, 4\}$  and  $B = \{0, 1, 2, 3\}$ .
- 2) Write in extension :  $A \cap B$  and  $A \cup B$ .
- 3) Complete by  $\in, \notin, \subset, \not\subset$  :
  - i.  $-4 \dots\dots A$
  - ii.  $\{1; 4\} \dots\dots A$ .

**Question III : (3pts)**

Solve the following system: 
$$\begin{cases} (x+1)(x^2+1) > 0 \\ \frac{4x^2 - 25 - 3(2x-5)}{x+4} \leq 0 \end{cases}$$

**Question IV : (4.5 pts) (the 2 parts are independent)**

1) Given :  $3 \leq x \leq 4$  and  $-2 \leq y \leq -1$ , and  $E = \frac{2x-1}{x^2+y^2}$ . Show that  $\frac{1}{4} \leq E \leq \frac{7}{10}$

2) Simplify: a)  $\frac{9^{\frac{2}{5}} \times 6^{\frac{3}{5}}}{\sqrt[5]{9} \times \sqrt[5]{2^3} \times \sqrt[5]{3^3}}$

b)  $\sqrt{(\sqrt{7}-3)^2} + \sqrt[3]{(2\sqrt{7}-5)^3} - |2-\sqrt{7}|$

**Question V : ( 6.5 pts) ( the four parts are independent )**

- 1) Simplify:  $\sin(7\pi - x) - \cos(-9\pi - x) - \cos\left(\frac{9\pi}{2} - x\right) + \tan\left(\frac{14\pi}{2} + x\right)$
- 2) Show that :  $\tan^2 x - \sin^2 x = (\tan^2 x)(\sin^2 x)$
- 3) Simplify :  $\cos^2 31^\circ + \cos^2 59^\circ - \cos 120^\circ$
- 4) Given :  $(\sin x + \cos x)^2 = \frac{5}{4}$ , where  $x \in [\pi, \frac{3\pi}{2}]$ 
  - i. Show that :  $\sin x \cdot \cos x = \frac{1}{8}$
  - ii. Calculate  $\frac{1}{\sin x} + \frac{1}{\cos x}$

**Question VI : (5.5 pts)**

In a system  $(O; \vec{i}; \vec{j})$ , consider the points:  $A(2; 5)$  ;  $B(-2; 2)$  ;  $C(0; -4)$  .

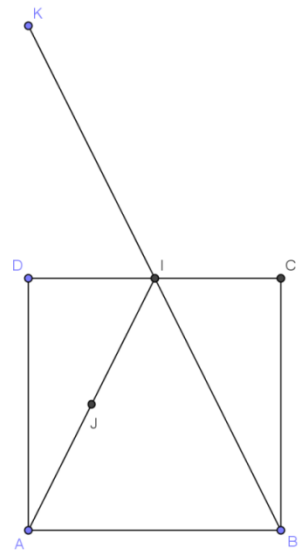
- 1) Find the coordinates of the vector  $\vec{V} = 2\vec{AB} - 3\vec{AC}$ .
- 2) Prove that  $A$  ,  $B$  and  $C$  determine a triangle.
- 3) Let  $M(2x+1; 2y+4)$  :
  - a- Calculate  $x$  and  $y$  if  $M$  is the centroid of the triangle  $ABC$  .
  - b- Find a relation between  $x$  and  $y$  if the vectors  $\vec{AM}$  and  $3\vec{AB}$  are collinear.
- 4) Find the coordinates of the point  $B(-2; 2)$  in the system  $(C; \vec{i}; \vec{j})$

**Question VII : ( 4 pts)**

ABCD is a square. The points I and J are respectively the midpoints of [DC] and [AI].

The point K is defined by:  $\vec{IK} = -\vec{IB}$

- 1) Redraw the figure
- 2) Show that :  $\vec{JK} = -\frac{1}{2}\vec{IA} - \vec{IB}$
- 3) Let L be a point defined by:  $2\vec{LA} + \vec{LB} = \vec{0}$ 
  - a) Verify that :  $\vec{AL} = \frac{1}{3}\vec{AB}$  . Construct L .
  - b) Show that :  $\vec{JL} = \frac{1}{6}\vec{IA} + \frac{1}{3}\vec{IB}$
  - c) Deduce that points K , J, and L are collinear .



GOOD WORK!