

1<sup>st</sup> exercise.

1.  $\cos \alpha = \frac{2\sqrt{2}}{3}$  And  $\cos^2 \alpha + \sin^2 \alpha = 1$  (Pythagorean identity)

$$\begin{aligned} \text{then, } \sin^2 \alpha &= 1 - \cos^2 \alpha \\ &= 1 - \left(\frac{2\sqrt{2}}{3}\right)^2 = 1 - \frac{8}{9} = \end{aligned}$$

$$\sqrt{\sin^2 \alpha} = \sqrt{\frac{1}{9}}$$

So,  $\sin \alpha = \pm \frac{1}{3}$  but  $\alpha$  is acute, hence  $\sin \alpha > 0$ .

$$\therefore \sin \alpha = \frac{1}{3} \quad \boxed{\text{Choice A}}$$

2.  $\vec{AM} + \vec{KA} + \vec{DK} + \vec{BD} + \vec{MB}$  (sum of consecutive vectors)  
 $= \vec{AM} + \vec{MB} + \vec{BD} + \vec{DK} + \vec{KA}$  (Use Chasles rule)  
 $= \vec{AA}$   
 $= \vec{0}$   $\boxed{\text{Choice C}}$

$$3. \frac{3x+2}{5} - \frac{2x+1}{3} \leq \frac{x+4}{3}$$

$$\frac{3x+2}{5} \leq \frac{x+4}{3} + \frac{2x+1}{3}$$

$$\left(\frac{3x+2}{5} \leq \frac{3x+5}{3}\right) \quad (\times 15)$$

$$9x+6 \leq 15x+25$$

$$(-6x \leq 19) \quad (\times -1)$$

$$6x \geq -19$$

$$\text{so } x \geq \frac{-19}{6}$$

hence  $x \geq -3.166\dots$

$\therefore$  The negative integers that satisfy the given inequality are  $-3, -2, -1 \neq 0$

$$\boxed{\text{Choice B}}$$