

a) * In ΔAOE we have:
 $[OA]$ is perp. to $[AE]$ (proved)
 hence, ΔOAE is right at A

$$\left. \begin{array}{l} - OE = a \\ - OA = R \end{array} \right\} \text{(given)}$$

$$\text{but } R = \frac{a}{2} \text{ (proved)}$$

$$\text{then, } OA = \frac{1}{2} OE$$

thus, ΔOAE is semi-equilateral Δ at A . (hyp = 2 smallest side)

$$\begin{aligned} b) * AE &= \frac{\sqrt{3}}{2} \times \text{hyp} \text{ (side facing } 60^\circ \text{ of a semi-equid)} \\ &= \frac{\sqrt{3}}{2} \times OE \end{aligned}$$

$$AE = \frac{\sqrt{3}a}{2} \text{ cm}$$

b) * $[EA]$ & $[EC]$ are tangents to (C) at A & C respectively (given)
 $[AB]$ & $[BC]$ are tangents to (C) at B & C respectively (given)
 so, 2 tangents are issued from each pt. E & F to (C) .

* In ΔEOF we have:

- E is the pt. of intersection of the 2 tangents $[EA]$ & $[EC]$ (given)

- O is the center of (C) (given)

then, $[EO]$ is the bisector of \hat{AEC} (tangent theorem: ① st. line joining pt. of intersection of the 2 tangents & the center is the bisector of the angle formed by the 2 tangents)

- F is the pt. of intersection of the 2 tangents $[FC]$ & $[FB]$ (given)

- O is the center of (C) (given)