

4) since F is translate (image) of C by the vector translation
 a) $\vec{CA} + \vec{CM}$ (Given)

then, $\vec{CF} = \vec{CA} + \vec{CM}$

So, quadrilateral CAFM is a parm.
 but, C belongs to (BC), the perp. bisector of [AM].
 then, C is equidistant from extremities A + M.
 hence, $CA = CM$.

Thus, parm CAFM is a rhombus (parm + equal adj. sides)

5) F is the 4th vertex of rhombus CAFM (proved)
 then, $\vec{CA} = \vec{MF}$

So, $X_{\vec{CA}} = X_{\vec{MF}} \quad \wedge \quad Y_{\vec{CA}} = Y_{\vec{MF}}$

$$\begin{aligned} x_A - x_C &= x_F - x_M \\ +1 &= x_F + 6 \\ x_F &= -5 \end{aligned}$$

$$\begin{aligned} y_A - y_C &= y_F - y_M \\ -7 &= y_F + 2 \\ y_F &= -9 \end{aligned}$$

Thus, $F(-5, -9)$

5) In right Δ ACH. apply Pythagorean theorem to find CH.

$$\begin{aligned} AC^2 &= AH^2 + CH^2 \\ \text{So, } CH^2 &= AC^2 - AH^2 \\ &= 50 - 10 \\ \sqrt{CH^2} &= \sqrt{40} \\ CH &= 2\sqrt{10} \text{ units of length} \end{aligned}$$

$$\begin{aligned} \tan \hat{CAH} &= \frac{\text{OPP}}{\text{hyp}} = \frac{CH}{AH} = \frac{2\sqrt{10}}{\sqrt{10}} \\ \therefore \tan \hat{CAH} &= 2 \\ \text{And, } \hat{CAH} &= \tan^{-1} 2 \\ \hat{CAH} &\approx 63.4^\circ \end{aligned}$$