

3 In $\triangle ABN$ we have:

(i) (OF) parallel to (AN) (given)

O is center of (C) of diameter $[AB]$ (given)

(ii) then O is midpt of $[AB]$

(iii) Thus, F is mid pt of $[BN]$ (by converse of midpt theorem in any \triangle)

4) a) In quadrilateral $AIBN$ we have

I is the pt of intersection of (C) & (AM) (given)

so, I is a pt on (C) of diameter $[AB]$

(i) then, $\hat{AIB} = 90^\circ$ (inscribed angle facing diameter)

(ii) $\hat{IAN} = 90^\circ$ (proved)

hence, (AN) is parallel to (IB) (st. lines held by equal corresponding angles)

(iii) Thus, $ANBI$ is a right trapezoid having a pair of parallel sides & a leg as a common height for both bases.

b) In \triangle 's AIB & FOB we have:

(i) $\hat{AIB} = 90^\circ$ (proved) } so, $\hat{AIB} = \hat{OBF}$ (by comparison)
 $\hat{OBF} = 90^\circ$ (proved)

(ii) $(IB) \parallel (AN)$ (proved) } so, (EF) is parallel to (IB)
 $(EF) \parallel (AN)$ (given) } (A pair of st. lines parallel to same st. line are parallel)

hence, $\hat{FOB} = \hat{IBA}$ (alt. interior angles held by parallel st. lines)

Thus, \triangle 's AIB & FOB are similar by Angle-Angle postulate.