

4) $\triangle AFB$ is inscribed in (c) ($A, F,$ and B are pts of (c)) ^{given}
 so, $\angle AFB = 90^\circ$ (inscribed angle facing diameter $[AB]$) ^{given}
 \rightarrow but $\triangle KAB$ is isosceles at K (proved)
 So, $\angle KAB = \angle KBA = 30^\circ$ (base angles in an isosceles \triangle)
 and F, K and B are collinear (given); $FA = FB$ (given)
 $\therefore \triangle FAB$ is isosceles (inscribed angle facing FB)

hence, $\triangle FAB$ is semi-equilateral at F having a 30° and a 90° angles.

$$\text{Thus, } FA = \frac{\text{hyp}}{\sin 30^\circ} \text{ (angle facing } 30^\circ)$$

$$= \frac{AB}{\sin 30^\circ} = \frac{2R}{\sin 30^\circ} \text{ (diameter} = 2r)$$

$$\boxed{FA = R \text{ cm}}$$

5) (AM) is perpendicular to (IB) at M (proved)
 (FB) is perpendicular to (AI) at F (proved)
 (KO) is the perpendicular bisector of (AB) (proved)
 They all intersect at K in $\triangle IAB$ (given - collinearity)
 Thus, K is the **ortho**-center of $\triangle IAB$

$\triangle IAB$ is an equilateral triangle since it has 2 angles 60° ($\angle IAB = \angle MBA = 60^\circ$ - proved) So, the perpendicular bisector of $[AB]$ pass through the vertex I .