

Thus, D is midpt of $[AF]$ (by converse of mid pt theorem in any Δ)

3) $FC = 2OD$ (by mid pt theorem in ΔAFC)

but $[OD]$ is a radius of (C)

And $AC = 10$ cm (diameter of (C))

So, $OD = \frac{AC}{2}$ (radius & diameter of same circle)

$$OD = 3 \text{ cm}$$

Hence $FC = 6 \text{ cm}$

In ΔADC we have:

D is a pt of (C) with diameter $[AC]$ (given)

So, $\hat{ADC} = 90^\circ$ (inscribed angle facing diameter)

$\hat{DAC} = 30^\circ$ (proved)

So, ΔADC is semi equilateral at D . (having $90^\circ + 30^\circ \angle$ s)

hence $AD = \frac{\sqrt{3}}{2} \text{ hyp}$ (side facing 60°)

$$= \frac{\sqrt{3}}{2} (AC)$$

$$AD = 5\sqrt{3} \text{ cm}$$

but D is mid pt of $[AF]$ proved.

Thus, $AF = 2AD$

$$AF = 10\sqrt{3} \text{ cm}$$

In ΔADI we have:

$\hat{DAI} = 30^\circ$, $\hat{DIA} = 90^\circ$ (proved)

So ΔADI is semi equilateral at I .

Thus, $AI = \frac{\sqrt{3}}{2} \text{ hyp}$ (①)

$$AI = \frac{\sqrt{3}}{2} AD = \frac{\sqrt{3}}{2} (5\sqrt{3}) = 7.5 \text{ cm}$$