

4) a)  $\triangle AOD$  is isosceles at  $O$  (proved).

$M$  is midpt of  $[AD]$  (given)

then,  $[OM]$  is a median relative to  $[AD]$ .

Thus  $[OM]$  is the perpendicular bisector of  $[AD]$

(median issued from main vertex of iso.  $\triangle$ ).

b) Since pts  $A+O$  are fixed

and  $\widehat{AMO} = 90^\circ$  (

Thus, as  $D$  varies on  $(C)$   $M$  describes a circle of diameter  $[AO]$  and center midpt of  $[AO]$ .

c)  $G$  is centroid of  $\triangle ADC$  (given).

$O$  is midpt of  $[AC]$  (proved)

then,  $[DO]$  is a median relative to  $[AC]$ .

Hence,  $OG = \frac{1}{3} OD$  (ratio  $\uparrow$  <sup>formed by</sup> centroid and median in a triangle).

$OG = 1\text{cm}$  which is constant.

Now,  $O$  is fixed

$G$  is variable

which means distance between a fixed pt and a variable pt is constant.

Thus as  $D$  moves on  $(C)$   $G$  trace a circle of center  $O$  & radius  $OG = 1\text{cm}$ .

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