

4) case of increase then decrease:

$$\text{final price} = \left(1 + \frac{\% \text{ increase}}{100}\right) \left(1 - \frac{\% \text{ decrease}}{100}\right) \times \text{initial price}$$

$$\frac{\text{final price}}{\text{initial price}} = \left(1 + \frac{25}{100}\right) \left(1 - \frac{\% d}{100}\right)$$

But final price equals initial price ✓

$$\text{Then, } (1 + 0.25) \left(1 - \frac{\% d}{100}\right) = 1 \quad \checkmark$$

$$(1.25) \left(1 - \frac{\% d}{100}\right) = 1 \quad \checkmark$$

$$1 - \frac{\% d}{100} = \frac{1}{1.25} \quad \checkmark$$

$$1 - \frac{\% d}{100} = 0.8$$

$$\frac{\% d}{100} = 1 - 0.8$$

$$\frac{\% d}{100} = 0.2 \quad \checkmark$$

$$\boxed{\% d = 20\%} \quad \textcircled{B} \quad \checkmark$$

5) (TA) & (TB) are two tangents to (C) at A & B resp.
So, TA = TB (tangent theorem: pt of intersection of 2 given tangents is equidistant from pts of tangency)

$$\text{Then } TA = 4 \quad \checkmark$$

But (OA) is a radius of (C) (given)

So, $\angle TAO = 90^\circ$ (tangent theorem: angle between tangent & radius is 90°) ✓

Then $\triangle TAO$ is right at A

use pythagorean theorem

$$\text{hyp}^2 = \text{leg}_1^2 + \text{leg}_2^2$$

$$TO^2 = TA^2 + OA^2$$

$$TO^2 = 4^2 + 3^2$$

$$\sqrt{TO^2} = \sqrt{25}$$

$$\boxed{TO = 5\text{cm}} \quad \checkmark$$