

\Rightarrow $[AC]$ is the diameter of the circle circumscribed about $\triangle ABC$

So radius = $\frac{AC}{2}$

But, $AC^2 = AB^2 + BC^2$ (Pythagoras theorem).

$AC^2 = (4 + \sqrt{7}) + (4 + \sqrt{7})$

$AC^2 = 8 + 2\sqrt{7}$

but $8 + 2\sqrt{7} = (\sqrt{7} + 1)^2$

$\Rightarrow AC^2 = (\sqrt{7} + 1)^2$

$\Rightarrow AC = \sqrt{7} + 1$

$\therefore r = \frac{\sqrt{7} + 1}{2}$

3rd exercise:

1) 1 is a root for $P(x)$

$\Rightarrow P(1) = 0$

$\Rightarrow 3(1)^3 - 12(1)^2 - 3(1) + a = 0$

$3 - 12 - 3 + a = 0$

$\therefore a = 12$

2) $P(x) = \underline{3x^3} - \underline{12x^2} - \underline{3x} + \underline{12}$

$= 3x(x^2 - 1) - 12(x^2 - 1)$

$= (x^2 - 1)(3x - 12)$

$\therefore P(x) = 3(x - 1)(x + 1)(x - 4)$

Now, $P(x) = 0$

$\Rightarrow 3(x - 1)(x + 1)(x - 4) = 0$

So, $x - 1 = 0 \Rightarrow x = 1$

or $x + 1 = 0 \Rightarrow x = -1$

or $x - 4 = 0 \Rightarrow x = 4$