

4) To compare a and b , we square both of them:

$$a^2 = \left(-\frac{\sqrt{2+\sqrt{3}}}{2}\right)^2$$
$$= \frac{2+\sqrt{3}}{4} \quad (2+\sqrt{3} > 0) \checkmark$$

$$b^2 = \left(\frac{\sqrt{2} + \sqrt{6}}{4}\right)^2$$
$$= \frac{8 + 2\sqrt{2 \times 3}}{16}$$
$$= \frac{8 + 4\sqrt{3}}{16} = \frac{4(2+\sqrt{3})}{16} = \frac{2+\sqrt{3}}{4}$$

$$a^2 = b^2 = \frac{2+\sqrt{3}}{4}$$

So, $a^2 - b^2 = 0$ (the difference of 2 equal nbs is 0)
then, $(a+b)(a-b) = 0$ but a is negative
So, $\boxed{a = -b}$ (True)

5) for $P(x)$ to be 3rd degree, the leading coefficient shouldn't be zero.

$$\text{So, } (m^2 - 3) \neq 0$$
$$(m - \sqrt{3})(m + \sqrt{3}) \neq 0$$

So, $m \neq \sqrt{3}$ and $m \neq -\sqrt{3}$ for $P(x)$ to be a 3rd degree trinomial

then $P(x)$ is a 3rd degree polynomial for all real values of m except for $m = \sqrt{3}$ or $m = -\sqrt{3}$.

(False)