

EX3

4) ICF of the value 3 sheets = $n_1 + n_2 + n_3 = 18 + 54 + 60 = 82$
 its meaning is: 82 students used at most 3 double sheet papers $(\frac{1}{4}, \frac{1}{2})$

5) a) $\bar{x} = \frac{n_1 x_1 + n_2 x_2 + n_3 x_3 + n_4 x_4}{N} = \frac{1 \times 18 + 2 \times 54 + \dots + 4 \times 8}{90}$
 $= \frac{188}{90} = 2.09 \approx 2$ double sheet papers $(\frac{3}{4} \text{ pt})$

b) $y_i = 2x_i$ so new mean $\bar{y} = \frac{y_1 n_1 + y_2 n_2 + y_3 n_3 + y_4 n_4}{N}$
 $= \frac{2x_1 n_1 + 2x_2 n_2 + 2x_3 n_3 + 2x_4 n_4}{N} = 2 \frac{(x_1 n_1 + x_2 n_2 + x_3 n_3 + x_4 n_4)}{N}$

$\bar{y} = 2\bar{x} = 2 \times \frac{188}{90} = \frac{188}{45}$ double sheet papers $(\frac{3}{4} \text{ pt})$

EX4

1) draw the orthogonal system. (1 pt)

2) $y_H = 2x_H + 4$
 $2 = 2(a-1) + 4$

$2 - 4 = 2a - 2$ so $2a = 0$ so $a = 0$

$H(-1, 2)$ $(\frac{3}{4} \text{ pt})$

3a) $y_M = 0$ so $0 = 2x_M + 4$ then $x_M = -2$ so $M(-2, 0)$

$x_N = 0$ so $y_N = 2(0) + 4 = 4$ then $N(0, 4)$

b) $\overrightarrow{MN} = \begin{pmatrix} x_N - x_M \\ y_N - y_M \end{pmatrix} = \begin{pmatrix} 0 - (-2) \\ 4 - 0 \end{pmatrix} = \begin{pmatrix} 2 \\ 4 \end{pmatrix}$

$2\overrightarrow{MH} = \begin{pmatrix} x_H - x_M \\ y_H - y_M \end{pmatrix} = \begin{pmatrix} -1 - (-2) \\ 2 - 0 \end{pmatrix} = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$

$2\overrightarrow{MH} = \begin{pmatrix} 2 \\ 4 \end{pmatrix}$ so $2\overrightarrow{MH} = \overrightarrow{MN}$

so $\overrightarrow{MN} = 2\overrightarrow{MH}$ then H is the midpt of $[MN]$ $(\frac{3}{4}, \frac{1}{4})$

4) a) $a_{(EH)} = \frac{y_H - y_E}{x_H - x_E} = \frac{2 - 4}{-1 - 1} = \frac{-2}{-2} = 1$ not defined so

(EH) has eq of $x = -1$ since E and H have same abscissa $(\frac{1}{4}, \frac{1}{4}, \frac{1}{2})$

