

4) $\cos 60^\circ = \frac{1}{2} \Rightarrow \sin 45^\circ = \frac{\sqrt{2}}{2}$

$68^\circ + 22^\circ$ are complementary angles (their sum equals 90°)

so, $\tan 68^\circ \times \tan 22^\circ = 1$ ($\tan \alpha \times \tan \beta = 1$ iff $\alpha + \beta = 90^\circ$)

Then $A = \frac{2(\cos 60^\circ + \sin 45^\circ)}{\tan 68^\circ \times \tan 22^\circ} \times (\sqrt{6} - \sqrt{3}) = \frac{2(\frac{1}{2} + \frac{\sqrt{2}}{2})(\sqrt{6} - \sqrt{3})}{1} = (1 + \sqrt{2})(\sqrt{6} - \sqrt{3})$

$A = \sqrt{3}$

Now, $A \times B = \sqrt{3} \times \frac{\sqrt{3}}{3} = 1$

Thus, A & B are reciprocal of each other

3rd ex:

1) population: Family

The character: Monthly expenses

The Modalities are: Food, transportation, housing, clothing, energy, schooling, entertainment

Nature: is qualitative since it can't be measured.

2)

Monthly expenses	Food	transportation	housing	clothing	energy	schooling	Entertainment	Total
Frequency	525000	$\frac{10 \times 1750000}{100} = 175000$	350000	140000	192500	202500	105000	1750000
% P	30	10	20	8	11	15	6	100%

3) NO, we can't find I. Cumulative frequencies since variable is qualitative

