

3rd - exercise:

1) a. $P(x) = 4(x-3)^2 - (x+1)^2$

$P(x) = [2(x-3)]^2 - (x+1)^2$ which is of the form $a^2 - b^2$.

$$P(x) = [2(x-3) - (x+1)][2(x-3) + (x+1)]$$

$$\therefore \boxed{P(x) = [x-7][3x-5]}$$

b. $Q(x) = (x-7)^2 - (x+1)(7-x) - 49 + x^2$

$$= (x-7)^2 + (x+1)(x-7) + (x^2 - 7^2)$$

$$= (x-7)^2 + (x+1)(x-7) + (x-7)(x+7)$$

$$= (x-7)[(x-7) + (x+1) + (x+7)]$$

$$\therefore \boxed{Q(x) = (x-7)(3x+1)}$$

c. $Q(-\frac{1}{3}) = (-\frac{1}{3} - 7)(3(-\frac{1}{3}) + 1)$
 $= (-\frac{1}{3} - 7)(0)$

$$\therefore Q(-\frac{1}{3}) = 0.$$

now, $P(-\sqrt{2}) = (-\sqrt{2} - 7)(3(-\sqrt{2}) - 5)$

$$= +6 + 5\sqrt{2} + 21\sqrt{2} + 35$$

$$P(-\sqrt{2}) = 41 + 26\sqrt{2}$$

$$\therefore Q(-\frac{1}{3}) + 110 > P(-\sqrt{2})$$

2) a. $P(x) = (x-7)(3x-5)$

$$= 3x^2 - 5x - 21x + 35$$

$$\therefore \boxed{P(x) = 3x^2 - 26x + 35} \text{ where } a=3; b=-26 \text{ \& } c=35$$