

3rd exercise 1) In $\triangle ABC$ we have

$ABCD$ is a rectangle (given)

So, $\hat{CBA} = 90^\circ$ (angle formed by adj. sides of a rect)

or $\hat{BAC} = 30^\circ$ (given)

Hence, $\triangle ABC$ is semi equilateral of hyp $[AC]$.

Thus, $AB = \frac{\sqrt{3}}{2} \text{ hyp}$ (side facing 60°)

$$= \frac{\sqrt{3}}{2} AC$$

$$= \frac{\sqrt{3}}{2} (4\sqrt{3}) / 2$$

$$\boxed{AB = \frac{12\sqrt{3}}{2}} = 6\text{ cm}$$

(1)

$$BC = \frac{1}{2} \text{ hyp}$$

$$BC = 2\sqrt{3} \text{ cm}$$

$$= \frac{1}{2} AC$$

(1)

But, $AD = BC$ opp. sides of a rect

Thus, $BC = AB = 2\sqrt{3} \text{ cm}$

2) In $\triangle EFB$ we have:

a) $\hat{EBF} = 90^\circ$ (proved)

So, $\triangle EFB$ is right at B.

$$(EB)^2 = \left(\frac{\sqrt{6} + \sqrt{2}}{2} \right)^2$$

$$EB^2 = \frac{6 + 4\sqrt{3} + 2}{4}$$

$$= \frac{8 + 4\sqrt{3}}{4}$$

$$EB^2 = (2 + \sqrt{3})^2$$

(4)

$$(FB)^2 = (\sqrt{2} + \sqrt{3})^2$$

$$FB^2 = 2 + \sqrt{3}$$

So, $FB^2 = EB^2$

Comparing \Rightarrow we see it's the same
as comparing their squares