

2nd exercise:

Part A:

$$1. EA = 3\sqrt{2}(\sqrt{3}+1) + (\sqrt{2}-1)(\sqrt{2}-2) - 4$$
$$= 3\sqrt{6} + 3\sqrt{2} + 2 - 2\sqrt{2} - \sqrt{2} + 2 - 4$$

$$EA = 3\sqrt{6} \text{ cm}$$

where $a=b$ & $b=6$

$$2. * AB = 8\sqrt{6} - 2\sqrt{3} \times \sqrt{2} + 2\sqrt{50}$$
$$= 8\sqrt{6} - 2\sqrt{6} + 2\sqrt{5^2 \times 6}$$
$$= 8\sqrt{6} - 2\sqrt{6} + 10\sqrt{6}$$

$$AB = 16\sqrt{6}$$

[AB] is a diameter of (C) of center O (given)

$$\text{then } R = \frac{AB}{2}$$

$$= \frac{16\sqrt{6}}{2}$$

$$R = 8\sqrt{6} \text{ cm}$$

$$3. * EO = EA + AO \quad (\text{E belongs to } [OA])$$

$$= 3\sqrt{6} + 8\sqrt{6}$$

$$EO = 11\sqrt{6} \text{ cm}$$

In $\triangle EPO$:

Apply converse of Pythagorean theorem:

$$\text{hyp}^2 \stackrel{?}{=} \text{leg}_1^2 + \text{leg}_2^2$$

$$EO^2 \stackrel{?}{=} OP^2 + EP^2$$

$$(11\sqrt{6})^2 \stackrel{?}{=} (8\sqrt{6})^2 + (3\sqrt{38})^2$$

$$726 \stackrel{?}{=} 384 + 342$$

$$726 = 726$$

So, $\triangle EPO$ is right \triangle at P

hence, [EP] and [OP] are perp. at P

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