

but [OP] is a radius (given)

thus, (EP) is tangent to (C) at P. (tangent theorem: tangent & radius are perp. at pt of tangency)

Part B:

$$1) EP = \frac{9ab - 15b + 3a - 5}{3a(3b+1) - 5(3b+1)}$$

$$EP = (3a-5)(3b+1) \text{ cm}$$

$$2) * EQ = (b+1)^2 + (2b+1)(3b-1) + (b+1)(2b+1) \\ = b^2 + 2b + 1 + 6b^2 - 2b + 3b - 1 + 2b^2 + b + 2b + 1$$

$$EQ = 9b^2 + 6b + 1$$

$$* EQ = 9b^2 + 6b + 1$$

$$= (3b)^2 + 2(3b)(1) + 1^2$$

$$EQ = (3b+1)^2$$

3) a - E is the pt. of intersection of the 2 tangents [EP] & [EQ] (given) then, E is equidistant from P & Q (tangent theorem, pt. of intersection of the 2 tangents is equidistant from pts. of tangencies).

$$\text{so, } EP = EQ$$

$$b - EP = EQ$$

$$[3(2) - 5][3b+1] = (3b+1)^2$$

$$(6-5)(3b+1) = (3b+1)^2$$

$$(3b+1) - (3b+1)^2 = 0$$

$$(3b+1)(1 - 3b - 1) = 0$$

$$(3b+1)(-3b) = 0$$

$$3b+1=0 \text{ or } -3b=0$$

$$b = -\frac{1}{3} \text{ or } b=0 \rightarrow \text{accepted}$$

$b = -\frac{1}{3}$  is rejected since it vanishes EQ

that is, geometrically this means that E will be a pt of tangency