

4th exercise: 1a) Drawn.

b):  $\vec{AD}(4,3)$ . (given)

ABCD is a parallelogram. (given)

$$\text{So, } \vec{AD} = \vec{BC} \quad \checkmark$$

$$\text{then } x_{AD} = x_{BC} \quad \checkmark \quad \text{or} \quad y_{AD} = y_{BC}$$

$$4 = x_C - x_B$$

$$3 = y_C - y_B$$

$$x_C = 8$$

$$y_C = 2$$

$$C(8,2) \quad \checkmark$$

c)  $C(8,2)$ .

$$\checkmark \text{ Slope}(BD) = \frac{y_D - y_B}{x_D - x_B} = 7$$

$$\checkmark \text{ Slope}(AC) = \frac{y_C - y_A}{x_C - x_A} = -\frac{1}{7}$$

$$\text{Slope}(BD) \times \text{Slope}(AC) = -1$$

Thus,  $(BD) \perp (AC)$  are perpendicular.  $\checkmark$

d) ABCD is a parm (given)

diagonals  $(BD) \perp (AC)$  are perpendicular (proved)

$\checkmark$  then ABCD is a rhombus (parm + perp. diagonals)

$$\text{but } AC = \sqrt{(x_B - x_A)^2 + (y_B - y_A)^2} \quad \checkmark \quad \text{or} \quad BD = \sqrt{(x_D - x_A)^2 + (y_D - y_A)^2}$$
$$= 5 \text{ units} \quad \checkmark \quad = 5 \text{ units}$$

$$\text{hence } AB = AD = 5 \text{ units} \quad \checkmark$$

Thus, rhombus ABCD is a square (rhombus + equal diagonals.)

2) a) Drawn

b) For  $(S)$  &  $(S')$  to be tangent externally, then distance between their centers A & B should be equal to the sum of their radii

$$\checkmark \text{ that is: } AB = r + r' \quad \checkmark$$

$$AB = 5 \text{ units}$$

$$\checkmark r + r' = 2 + 3 = 5 \text{ units}$$

$$\text{Hence } AB = r + r' = 5 \text{ units} \quad \checkmark$$

Thus,  $(S)$  &  $(S')$  are tangent externally at E.