

* 5th Exercise:

2. In $\triangle ABC$ we have:

$$AB = AC \text{ (given)}$$

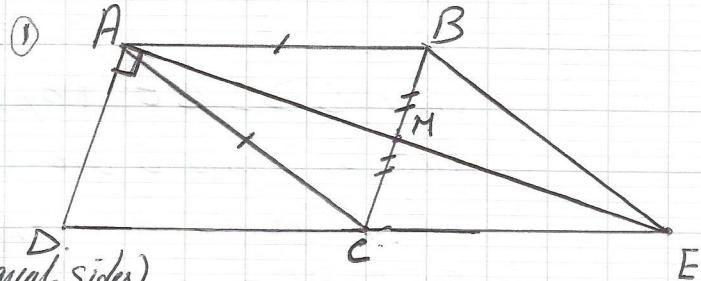
then, $\triangle ABC$ is isosceles.

of vertex A (having a pair of equal sides)

but M is midpt of $[BC]$ (given).

then $[AM]$ is a median relative to $[BC]$.

Thus, (AM) is perpend BC) (Median issued from main vertex of an isosceles \triangle is a height as well).



3. Consider quadrilateral ABEC:

M is midpt of $[BC]$ (given)

E is symmetric of A w.r.t M (given)

then M is mid pt of $[AE]$.

So, quad ABEC is a parallelogram (having its diagonals bisect each other at same mid pt).

But $AB = AC$ (given)

Therefore, parallelogram ABEC is a rhombus (having a pair of adjacent sides equal).

4. $(AB) \parallel (DC)$ (opposite sides of para ABCD)

$(AB) \parallel (CE)$ (opposite sides of rhombus ABEC)

then, $(DC) \parallel (CE)$ (Two lines parallel to same line are parallel)

but C is a common point.

Thus, points D, C and E are collinear.