

$$\begin{aligned} \text{Area } \triangle DOB &= \frac{\text{leg}_1 \times \text{leg}_2}{2} \\ &= \frac{DB \times OB}{2} \\ &= \frac{R\sqrt{3} \times R}{2} \\ &= \frac{R^2\sqrt{3}}{2} \end{aligned}$$

$$\begin{aligned} \text{Area of } \triangle DCB &= \frac{\text{leg}_1 \times \text{leg}_2}{2} \\ &= \frac{BD \times CB}{2} \\ &= \frac{R\sqrt{3} \times \frac{4R}{3}}{2} \\ &= \frac{4R^2\sqrt{3}}{6} \end{aligned}$$

$$\begin{aligned} \text{Thus, Area of } \triangle COD &= \frac{4R^2\sqrt{3}}{6} - \frac{R^2\sqrt{3}}{2} \\ &= \frac{5R^2\sqrt{3} - 3R^2\sqrt{3}}{6} \\ &= \frac{2R^2\sqrt{3}}{6} \text{ units of area.} \end{aligned}$$

2nd way: Area $\triangle COD = \frac{\text{base} \times \text{height}}{2} = \frac{CO \times BD}{2} = \frac{R}{3} \times \frac{R\sqrt{3}}{2} = \frac{R^2\sqrt{3}}{6} \cdot 4^2$

3) In quadrilateral $MNOB$ we have

• M is the orthogonal projection of B on $[CD]$ (given)

So, $\widehat{BMC} = 90^\circ$

• The perp. bisector of $[AB]$ at O cuts $[CD]$ in N (given)

So, $\widehat{NOB} = 90^\circ$

hence, quadrilateral $MNOB$ is formed of two right \triangle 's

Sharing the same hypotenuse $[NB]$

Thus, pts M, N, O & B belong to the same circle of center the midpt of its diameter $[NB]$.

4) $[DE]$ is tangent to (C) at E (given)

$[DB]$ is tangent to (C) at B (given) the

So, D is an exterior pt from which two tangents $[DB]$ & $[DE]$ are drawn to (C) of center O at B & E respectively

Thus, $[DO]$ is the bisector of \widehat{EDB} (tangent theorem: