

c) A belongs to x-axis (given)  
B belongs to y-axis (given)

x + y axes are perp. (orthonormal system)

$$\text{then, } \hat{A}OH + \hat{H}OB = 90^\circ$$

but,  $\hat{H}BO + \hat{H}OB = 90^\circ$  (base angles in right  $\triangle OBH$ )

Thus  $\hat{A}OH = \hat{H}BO$  (Two angles having the same complement are equal)

$$d) \cos \hat{A}OH = \frac{OH}{OA}; \sin \hat{O}BH = \frac{OH}{OB} \quad (\text{proved})$$

and  $\hat{A}OH = \hat{O}BH = \alpha$ . (given)

then,

$$\cos \alpha = \frac{OH}{OA} \quad \& \quad \sin \alpha = \frac{OH}{OB}$$

$$\text{but, } \cos^2 \alpha + \sin^2 \alpha = 1$$

$$\text{so, } \left(\frac{OH}{OA}\right)^2 + \left(\frac{OH}{OB}\right)^2 = 1$$

$$\left(\frac{OH^2}{4} + \frac{OH^2}{16} = 1\right) \times 16$$

$$5OH^2 = 16$$

$$OH = \frac{4}{\sqrt{5}} \quad (\text{OH represents a side})$$

$$\text{Thus, } OH = \frac{4\sqrt{5}}{5} \text{ cm.}$$

$$4a. \tan \hat{O}AB = \text{slope of } (d)$$

$$\tan \hat{O}AB = 2$$

$$\hat{O}AB = \tan^{-1}(2)$$

$$= 63.434^\circ$$

$$\approx 63.43^\circ \quad (\text{to nearest } 10^{-2})$$