

c) In $\triangle ABC$ we have:

M is midpt of $[BC]$ (proved)

→ then, $[AM]$ is a median relative to $[BC]$.

→ And $[AM]$ is perpendicular to $[BC]$ (given).

So, $[AM]$ is the perp. bisector of $[BC]$

hence, $\triangle ABC$ is isosceles of vertex A (having a perp. bisector passing through one of its vertices)

* $AM = \frac{BC}{2}$ (proved)

Thus, $\triangle ABC$ is right isosceles at A (property of a median relative to hyp of a right \triangle).

5) a) (Δ) is perp to (AC) (given).

$$\text{So, } a_{(\Delta)} \times a_{(AC)} = -1$$

$$\begin{aligned} \text{but } a_{(AC)} &= \frac{y_C - y_A}{x_C - x_A} \\ &= \frac{1 + 2}{6 - 2} \end{aligned}$$

$$a_{(AC)} = \frac{3}{4}$$

$$\text{hence } a_{(\Delta)} = -\frac{4}{3}$$

but, (Δ) passes through $K(3, 4)$

$$(\Delta): y - y_K = a_{(\Delta)} (x - x_K)$$

$$y - 4 = -\frac{4}{3} (x - 3)$$

$$(\Delta): y = -\frac{4}{3}x + 8$$

b) (L) passes through $(0, 2)$
and $(3, 0)$

(ordinate of origin is 2)
(x-intercept).

$$(L): \frac{y - y_1}{x - x_1} = \frac{y_2 - y_1}{x_2 - x_1}$$