

5) a) (n) is \perp (AB) (given).

\perp (AB) \perp (EF) .

So, $(n) \parallel (EF)$ (Two st. lines in plane perp. to same st. line are parallel)

$$\text{So } a_{(n)} = a_{(EF)} = 2$$

O belongs to (n) (given)

$$\text{So, } (n): \frac{y - y_0}{x - x_0} = a_{(n)}$$

$$\frac{y}{x} = 2$$

* Thus, $(n): y = 2x$.

b) D is the intersection pt of (n) & (AB) (given).

So, coordinates of D satisfies both eqns of (n) & (AB) at same time.

$$\begin{cases} y = 2x & \dots (1) \\ y = -\frac{x}{2} + \frac{3}{2} \end{cases}$$

$$y = y$$

$$(2x = -\frac{x}{2} + \frac{3}{2}) \times 2$$

$$4x = -x + 3$$

$$5x = 3$$

$$x = \frac{3}{5}$$

Sub. value of x in eqn (1)

$$y = 2x$$

$$y = 2\left(\frac{3}{5}\right)$$

$$y = \frac{6}{5}$$

Thus, $D\left(\frac{3}{5}, \frac{6}{5}\right)$.

c) In Δ 's ADO & AEB sharing same vertex A we have:

A, O & E are collinear (all on x -axis)

A, D & $B \parallel \parallel$ in this order.

$(EF) \parallel (n)$ (proved)

$(OD) \subseteq (n)$.

Then, $(EF) \parallel (n)$.