

2)  $M$  is a pt on  $(c)$  of diameter  $[AB]$  (given)  
So,  $\angle AMB = 90^\circ$  (inscribed angle facing diameter)  
So,  $(AM) \perp (MB)$

$P$  is the intersection pt. of the tangents  $[PB]$  &  $[PM]$  to  $(c)$   
at  $B$  &  $M$  respectively (given)

So,  $(OP)$  is the perp. bisector of  $[MB]$  (tangent theorem:  
st. line joining pt of intersection of two  
tangents to center of circle is perp. bisector  
of segment joining pts of tangencies)

So,  $(OP) \perp (MB)$

Thus,  $(OP)$  is parallel to  $(AM)$  (two st. lines perp. to same  
st. line are parallel).

3) In  $\triangle ABR$  we have:

$O$  is the center of  $(c)$  with diameter  $[AB]$  (given)

So,  $O$  is midpt of  $[AB]$ .

$\therefore (OP) \parallel (AM)$ . (proved)

but pts  $A, M$  &  $R$  are collinear (given)

so  $(OP) \parallel (AR)$ .

Thus,  $P$  is midpt of  $[BR]$  (by converse of midpt  
theorem in a  $\triangle$ ).

4a) In  $\triangle OQS$  we have:

$[SB]$  is a tangent to  $(c)$  at  $B$ . (given)

$[SM]$  is " " "  $(c)$  "  $M$  (given)

So,  $[SB]$  &  $[SM]$  are heights relative to  $[OS]$  and  $[QS]$   
respectively

but,  $[SB]$  &  $[SM]$  intersect at  $P$  (given)

so,  $P$  is the orthocenter of  $\triangle OQS$  (intersection pt of height)

And  $(OP)$  is issued from vertex & passes through  $P$ .