

4) a) In  $\triangle EAB$  we have:

$E$  is located on the perpendicular bisector of  $[AB]$  (given)

So,  $E$  is equidistant from  $A$  &  $B$

$$EA = EB.$$

So,  $\triangle EAB$  is isosceles at  $E$ .

But,  $\hat{A} = \hat{B} = 60^\circ$  (side of equilateral  $\triangle$ ).

~~As~~  $\hat{A}$  &  $\hat{B}$  are collinear,

$$\text{So, } \hat{E} = 60^\circ.$$

Thus,  $\triangle EAB$  is equilateral (isosceles  $60^\circ$ ).

b) Since  $EAB$  is an equilateral  $\triangle$  (proved)

So, any height issued from any of the 3 vertices is also the median.

~~Thus~~ Since,  ~~$\hat{B}$~~   $\hat{B} = 90^\circ$  (proved).

$[MB]$  is the height issued from  $B$  to  $[EA]$ .

Then,  $[MB]$  is also the median of  $[EA]$ .

So,  $M$  is the midpoint of  $[EA]$ .

c) In semi-equilateral  $\triangle EOA$  at  $O$  ( $90^\circ - 60^\circ$ ).

$[EO]$  side facing  $60^\circ = \text{side facing } 30^\circ \times \sqrt{3}$

$$EO = AO \times \sqrt{3}$$

$$EO = 6\sqrt{3} \quad \text{cm}$$

$$\text{Then, } OE = MB = 6\sqrt{3}$$