

- $\triangle MAB$ is an inscribed \triangle in (c) ($M, A,$ and B belong to (c) - given) having one of its sides - the diameter $[AB]$ (given)
- Then, $\angle AMB = 90^\circ$ (inscribed angle facing diameter)
- Thus, $\triangle MAB$ is semi-equilateral at M having a 90° and a 30° angle (proved).

b) $\triangle MAB$ is semi-equilateral at M (proved) So,

$$MB = \frac{\text{hyp}}{2} = \frac{AB}{2} = \frac{12}{2} \quad (d = d \text{ where } r = 6 \text{ cm - given})$$

$$= 6 \text{ cm (side facing } 30^\circ)$$

$$AM = \frac{\text{hyp} \sqrt{3}}{2} = \frac{AB \sqrt{3}}{2} = \frac{12\sqrt{3}}{2} = 6\sqrt{3} \text{ cm (side facing } 60^\circ)$$

3) a) $[MF]$ is tangent to (c) at M (given) and $[BF]$ is tangent to (c) at F (given), and they both intersect at F (given)

then, F is equidistant from M and B (tangent theorem: the exterior point is equidistant from the 2 points of tangency).

$$\text{So, } \boxed{FM = FB}$$

- $[AE]$ is tangent to (c) at A (given) and $[ME]$ is tangent to (c) at M (given).

So, E is equidistant from A and M (tangent theorem)

$$\text{then } \boxed{EA = EM}$$

but $EF = EM + MF$ ($E, M,$ and F are collinear - given)

thus, $EF = EA + FB$ (by comparison)