

1) Hence Δ 's $\triangle INE$ & $\triangle IME$ are congruent by RHA property.

Thus, $IN = IM$ (homologous elements)

3) In quadrilateral $INEM$ we have

1) $\angle INE = \angle IME = 90^\circ$ (proved).

2) hence quad is formed of 2 right Δ 's sharing same hypotenuse $[IE]$.

3) Thus, pts I, N, E, M belong to same circle whose diameter is the common hypotenuse $[IE]$ & center the midpt of $[IE]$.

4a) (c) is a circle of center E & radius, $[EM]$.

1) $\left\{ \begin{array}{l} E \text{ is a pt on } [IT], \text{ the bisector of } \angle I \hat{T} Y \text{ (given)} \\ EN \text{ & } EM \text{ are orth. projections of } E \text{ on } [IX] \text{ & } [IY] \text{ res p. (given)} \end{array} \right.$

2) then, E is equidistant from M & N
hence, EN is a radius of (c).

$IN = IM$ (proved)

3) Thus, (IN) & (IM) are tangents to (c) at N & M
(Tangent Theorem: Exterior pt from which two tangents are drawn to a circle is equidistant from pts of tangencies).

5) In ΔINM we have

1) $\angle MIN = 60^\circ$ (given) } 2) Thus, ΔINM is equilateral

3) $IN = IM$ (proved) } 4) (having two equal sides and $60^\circ \angle$)