

09

3rd exercise:

$$1) \text{ Area of } \triangle MCN = \frac{\text{Height} \times \text{base}}{2} \quad (\angle C = 90^\circ \text{ angle of rectangle})$$

(B, M, C)
&
(D, N, C)
collinear

$$= \frac{MC \times NC}{2}$$

$$= \frac{(2-x) \times (4-x)}{2}$$

$$= \frac{8 - 2x - 4x + x^2}{2}$$

$$A_1(x) = \frac{x^2 - 6x + 8}{2} \text{ cm}^2$$

$$2) a) \text{ Area of } \triangle DNA = \frac{\text{Height} \times \text{base}}{2} \quad (\angle D = 90^\circ \text{ angle of rectangle})$$

$$= \frac{AD \times DN}{2}$$

$$= \frac{2x}{2}$$

$$A_2(x) = x \text{ cm}^2$$

$$b) P(x) = A_1(x) + A_2(x)$$

$$= \left(\frac{x^2 - 6x + 8}{2} \right) + \left(\frac{x}{1} \right) \times 2$$

$$P(x) = \frac{x^2 - 6x + 8 + 2x}{2} = \frac{x^2 - 4x + 8}{2}$$

$P(x)$ is a second degree algebraic expression in terms of x

$$3) a) \text{ Area of shaded region} = \text{Area of rectangle} - (A_1(x) + A_2(x))$$

$$= \text{length} \times \text{width} - \left(\frac{x^2 - 4x + 8}{2} \right)$$

$$= AB \times AD - \left(\frac{x^2 - 4x + 8}{2} \right)$$

$$= \frac{8 \times 2}{1 \times 2} - \left(\frac{x^2 - 4x + 8}{2} \right)$$

$$= \frac{16 - x^2 + 4x - 8}{2}$$

P=8

$$E(x) = \frac{8 - x^2 + 4x}{2} = \frac{-x^2 + 4x + 8}{2}$$