

5.a) In quadrilateral AEOF we have:

F is the symmetric of E w.r.t (AB) (given)

then, (AB) is the perp. bisector of [EF].

then, $\boxed{AE = AF}$ --- (c)

And $\boxed{OE = OF}$ (radii of (C)) --- (a)

but (OE) \perp (PD) (proved)

$\angle E\hat{O}P = 30^\circ$ (proved)

So, $E\hat{O}P = 60^\circ$ (sum of angles in $\triangle EOP$) --- (b)

then, from (a) & (b) we get

$\triangle EOA$ is equilateral (having two equal sides + 60°)

hence, $AE = EO = OF = AF$ (by comparison)

Thus, quad. AEOF is a rhombus (having 4 equal sides)

b) AE is a rhombus (proved)

So, (AE) \parallel (FO). (Opp. sides of a rhombus are parallel)

but $\triangle EAO$ is an equilateral \triangle (proved)

So, $E\hat{A}O = 60^\circ$ (angle formed by sides of an equi \triangle)

but $D\hat{O}B = 60$ (given)

Then, (AE) \parallel (OD) (equal corresponding angles are held by parallel st. lines)

hence, (OD) \parallel (OF) (two st. lines parallel to same st. line

but O is a common pt. are parallel)

Thus, the pts O, D & F are collinear.

c) (AB) is perp. bisector of [EF] (proved)

but F & O belong to (AB) (given)

hence (FO) is the perp. bisector of [EF].

But, (EP) is tangent to (C) at E. (proved)

And F belong to (C).