

b) i)  $[FO]$  is the bisector of  $\hat{M}OB$   
 and  $[OE]$  is the bisector of  $\hat{MOA}$   
 (tangent theorem: the line joining the exterior pt. and the centre is the bisector of the central angle)  
 and  $\hat{MOB}$  and  $\hat{MOA}$  are 2 adjacent supplementary angles  
 ( $A, O,$  and  $B$  are collinear - given  $O$  is the center of  $(C)$  of diameter  $[AB]$ )  
 Thus,  $\hat{EOF} = 90^\circ$  (the angle formed between the bisectors of 2 adjacent supplementary angles is  $90^\circ$ )

ii)  $\hat{MOA} = 120^\circ$  (proved)  
 and  $[OE]$  is the bisector of  $\hat{MOA}$  (proved)  
 so,  $\hat{MOA} = 2\hat{MOE}$   
 $\hat{MOB} = 60^\circ$  (central angle intercepting  $\widehat{MB}, \widehat{MO} = 60^\circ$  - given)  
 and  $[OF]$  is the bisector of  $\hat{MOB}$  (proved)  
 so,  $\hat{MOB} = 2\hat{MOF}$

$\rightarrow \hat{AOB} = \hat{AOM} + \hat{MOB}$  (2 adjacent supplementary angles)  
 $180^\circ = 2\hat{MOE} + 2\hat{MOF}$  (proved)  
 $180^\circ = 2(\hat{MOE} + \hat{MOF})$   
 $\hat{MOE} + \hat{MOF} = 90^\circ$   
 thus,  $\hat{FOE} = 90^\circ$  ( $\hat{MOF}$  and  $\hat{MOE}$  are adjacent angles).

4) a)  $[OI]$  is the bisector of  $\hat{MOA}$  ( $O, I,$  and  $E$  are collinear)  
 so,  $\hat{IOA} = \frac{\hat{MOA}}{2} = \frac{120^\circ}{2}$  (proved) =  $60^\circ$ .

so,  $\triangle IOA$  is semi-equilateral at  $I$  having ( $30^\circ - 60^\circ$  angles)  
 then  $\hat{AIO} = 90^\circ$ , then  $(AM)$  is perpendicular to  $(IO)$  at  $I$   
 $\rightarrow \hat{BMA} = 90^\circ$  (proved), so  $(BM)$  is perpendicular to  $(AM)$

P-9.

$(A, I,$  and  $M)$  are collinear