

4) $[IM)$ & $[IN)$ are tangents drawn to (C) of center E at M & N respectively (proved)

then, $[EI)$ is the bisector of \widehat{NEM} (Tangent theorem: st. line joining center of circle & pt of intersection of tangents is bisector of central angles intercepting arc formed by pts of tangencies.)

hence, $\widehat{NEP} = \widehat{MEP}$.

hence, $\widehat{NP} = \widehat{MP}$ (arcs intercepting equal arcs)

Thus, P is midpt of \widehat{MN} .

5a) (IB) is perp. bisector of $[NM]$ (Tangent theorem: st. line joining center of circle and pt of intersection of tangents)

J is diametrically opp. of P (given)

then, J is a pt on (IB)

So, J is equidistant from pts M & N

So, $JN = JM$.

a) now, I, N, E & M belong to same circle (proved).

So, $\widehat{NIM} + \widehat{NEM} = 180^\circ$ (sum of opp. angles in an inscribed quadrilateral)

but, $\widehat{NIM} = 60^\circ$ (given)

hence, $\widehat{NEM} = 120^\circ$

So, $\widehat{NJM} = \frac{1}{2} \widehat{NEM}$ (central & inscribed angles intercepting same arc \widehat{MN} in (C))

Thus, $\widehat{NJM} = 60^\circ$