

➤ Sketching graphs by Translation

Functions	Relation between $f(x)$ & $g(x)$	Translation vector $\vec{s}(x; y)$	Sketching C_g using C_f by translation
1) $f(x) = x^2$		$g_k(x)$ is the translate of $f(x)$ by:	
$g_1(x) = x^2 + 2$	$g_1(x) = \dots\dots\dots$		
$g_2(x) = x^2 - 2$	$g_2(x) = \dots\dots\dots$		
$g_3(x) = (x - 1)^2$	$g_3(x) = \dots\dots\dots$		
$g_4(x) = (x + 1)^2$	$g_4(x) = \dots\dots\dots$		
$g_5(x) = (x + 1)^2 - 2$	$g_5(x) = \dots\dots\dots$		
2) $f(x) = \sqrt{x}$			
$g_1(x) = \sqrt{x} + 2$	$g_1(x) = \dots\dots\dots$		
$g_2(x) = \sqrt{x} - 2$	$g_2(x) = \dots\dots\dots$		
$g_3(x) = \sqrt{x - 1}$	$g_3(x) = \dots\dots\dots$		
$g_4(x) = \sqrt{x + 1}$	$g_4(x) = \dots\dots\dots$		
$g_5(x) = \sqrt{x + 1} - 2$	$g_5(x) = \dots\dots\dots$		
3) $f(x) = \frac{1}{x}$			
$g_1(x) = \frac{1}{x} + 2$	$g_1(x) = \dots\dots\dots$		
$g_2(x) = \frac{1}{x} - 2$	$g_2(x) = \dots\dots\dots$		
$g_3(x) = \frac{1}{x - 1}$	$g_3(x) = \dots\dots\dots$		
$g_4(x) = \frac{1}{x + 1}$	$g_4(x) = \dots\dots\dots$		
$g_5(x) = \frac{1}{x + 1} - 1$	$g_5(x) = \dots\dots\dots$		

Sketching of basic functions by Translation

A- Parabola:

The graph of $g : g(x) = (x - h)^2 + k$, is similar to that of the basic function,

$f : f(x) = x^2$ **Shifted:**

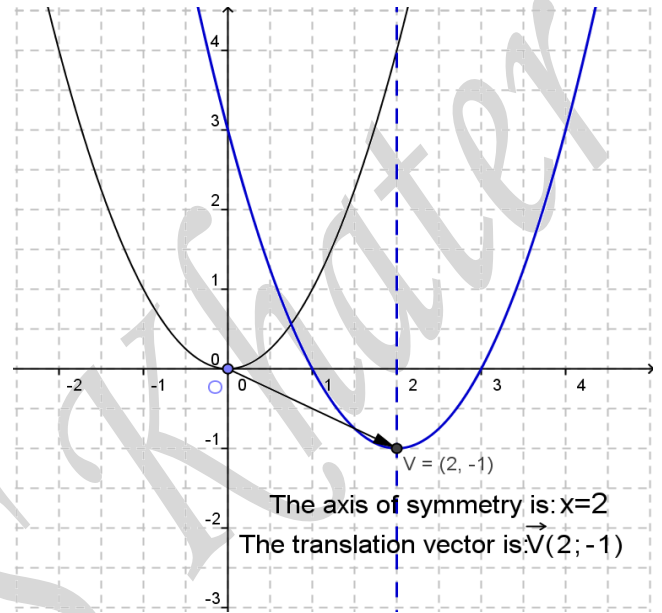
Horizontally h units to the		Vertically k units	
Right	If,	Upwards	If,
Left	If,	Downwards	If,

✓ **Note that:**

- The equation of translation is:

$$g(x) = f(x - h) + k$$

- The **translation vector** is:
- The **new** axis of symmetry is:
- The is $V(h, k)$



B- Absolute value function:

The graph of $g : g(x) = |x - h| + k$ is similar to that of the basic function:

$f : f(x) = |x|$ **Shifted:**

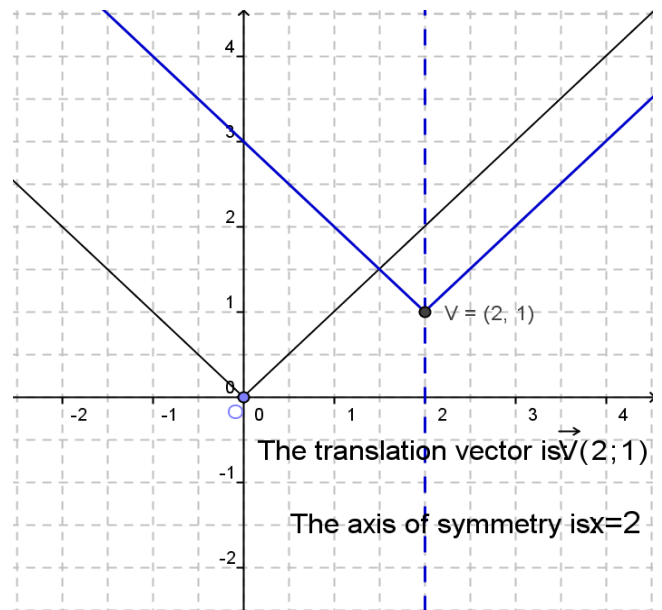
Horizontally h units to the		Vertically k units	
Right	If,	Upwards	If,
Left	If,	Downwards	If,

✓ **Note that:**

- The equation of translation is:

$$g(x) = f(x - h) + k$$

- The **translation vector** is $\vec{s}(h, k)$
- The is $x = h$
- The **new vertex** is:



C- Square root function:

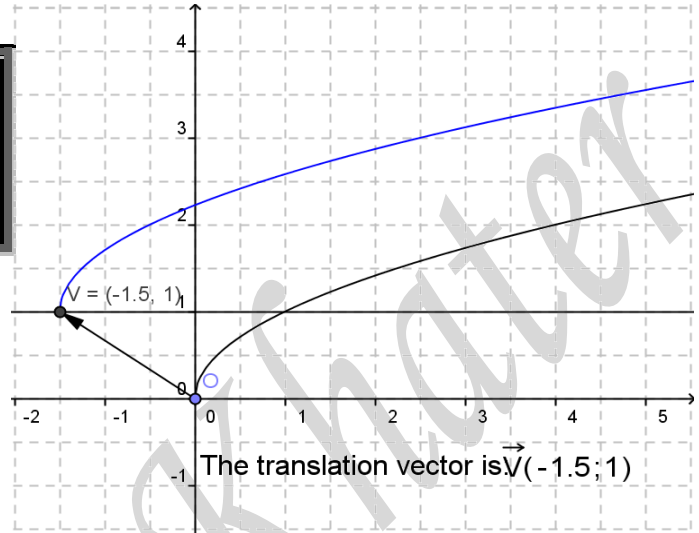
The graph of $g : g(x) = \sqrt{x-h} + k$ is similar to that of the basic function,

$f : f(x) = \sqrt{x}$ **Shifted:**

Horizontally h units to the		Vertically k units	
Right	If,	Upwards	If,
Left	If,	Downwards	If,

✓ **Note that:**

- The equation of translation is:
- The **translation vector** is:
- The is $x = h$
- The **new vertex** is:



D- Rational function:

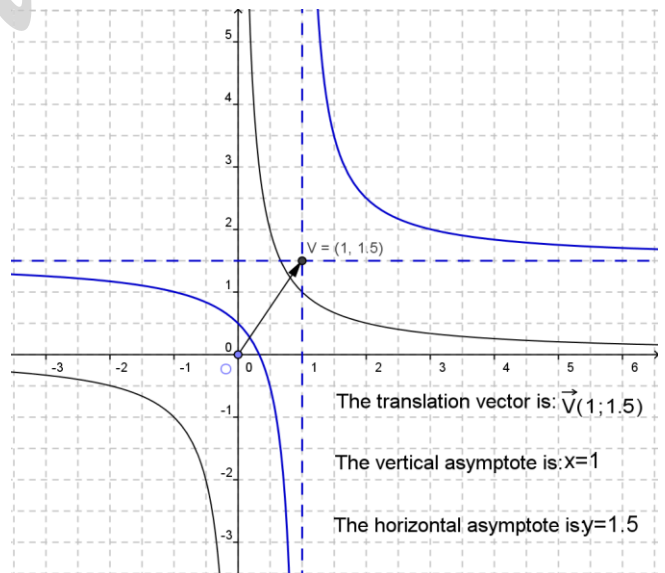
The graph of $g : g(x) = \frac{1}{x-h} + k$ is similar to that of the basic function,

$f : f(x) = \frac{1}{x}$ **Shifted:**

Horizontally h units to the		Vertically k units	
Right	If,	Upwards	If,
Left	If,	Downwards	If,

✓ **Note that:** C_g admits a

- **Translation vector** $\vec{v}(\dots, \dots)$
- center of symmetry $C(\dots, \dots)$
- **Vertical** asymptote of equation
- **Horizontal** asymptote of equation
- **New vertex** $V(\dots, \dots)$
- The **equation** of translation is:



➤ *Sketching graphs of basic functions by symmetry*

Functions	Relation between $f(x)$ & $g(x)$.	Type of symmetry between C_f & C_g .	Sketching C_g using C_f by symmetry
A. $f(x) = x^2$		(C_g) & (C_f) Are symmetric with respect to Since,.....	
$g(x) = -x^2$	$g(x) = \dots\dots\dots$		
B. $f(x) = \sqrt{x}$			
$g_1(x) = \sqrt{-x}$	$g_1(x) = \dots\dots\dots$		
$g_2(x) = -\sqrt{x}$	$g_2(x) = \dots\dots\dots$		
$g_3(x) = -\sqrt{-x}$	$g_3(x) = \dots\dots\dots$		
C. $f(x) = \frac{1}{x}$			
$g(x) = -\frac{1}{x}$	$g(x) = \dots\dots\dots$		
Conclusions			
If $\forall (x; y) \in C_f \exists (x; -y) \in C_g$ then C_f & C_g are symmetric w.r.t $x'ox$. OR $(x; y) \xrightarrow{\text{symm w.r.t } x'ox} (x; -y)$			
If $\forall (x; y) \in C_f \exists (-x; y) \in C_g$ then C_f & C_g are symmetric w.r.t $y'oy$. OR $(x; y) \xrightarrow{\text{symm w.r.t } y'oy} (-x; y)$			
Deduce the element of symmetry of a function around the origin:			