## Lycée Des Arts

## Mathematics

10th-Grade

Name: . . . . . . "Quadratic functions and inequalities "

S.S-14

The complete form of a quadratic function is given by:  $h(x) = ax^2 + bx + c$ 



To solve a quadratic inequality of the form  $ax^2 + bx + c < or > 0$ 



Write the given quadratic inequality in the form  $h(x) = (x - h)^2 + k$  "by completing the square"



Graph the function:  $h(x) = (x - h)^2 + k$  "carefully".



Specify the x-intercepts of h(x) "by solving  $(x-h)^2 + k = 0$ "



Detect • the sign of the inequality:



$$h(x) = ax^2 + bx + c > 0$$



$$h(x) = ax^2 + bx + c < 0$$

Then take values of x for which the graph is

**Strictly above** the x-axis

**Strictly below** the x-axis



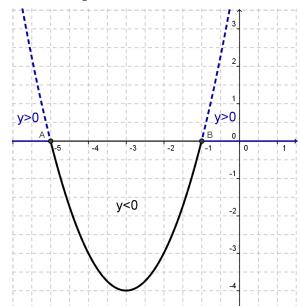
Solve graphically the following inequality:  $h(x) = x^2 - 6x + 5 \ge 0$ 

1<sup>st</sup> - Step: Change form:  $h(x) = x^2 - 6x + 5 = (x+3)^2 - 4$ , which is a parabola of vertex V(-3, -4)

 $2^{\text{nd}}$  - Step: Graph h(x)

 $3^{rd}$  – Step: Specify x-intercepts: A(-5;0) and B(-1;0).

 $4^{th}$  - Step: Detect given sign:  $h(x) \ge 0$ 



Thus,  $x \in ]-\infty;-5] \cup [-1;+\infty[$ 

