# MATHEMATICS (SEMESTER 1 -: 60) (SEMESTER 2 - 60 PERIODS)

# CHAPTER 1 CALCULUS

#### 1.1 Double integrals

- 1.1.1 Sum of integrals over closed domains a bounded and rectangular partitioned one
- 1.1.2 Geometric significance of a double integral
- 1.1.3 Conditions of the functions integrability over a closed bounded and rectangular domain
- 1.1.4 The rules of calculation by using simple integrals (Fubini's theorem)
- 1.1.5 Properties of double integrals
  - 1.1.5.1 Linearity of the double integral
  - 1.1.5.2 Integrability over the union of two non-overlapping domains
  - 1.1.5.3 Inequalities of double integrals
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- 1.1.6 Substitutions in double integrals
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- 1.2 Triple integral
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  - 1.2.5 Properties of triple integrals
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    - 1.2.5.3 Inequalities of triple integrals
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  - 1.2.6 Substitutions of variables into triple integrals. Geometric significance of a Jacobean
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- 2.1.1.6 Green formula, application over the Plainfield area
- 2.1.1.7 Conditions to frame a line integral free from the path, and depend on extremities
- 2.2 Surface integrals
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- 2.3 Vertical calculus
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  - 2.3.2 Divergence formula, physical interpretation rotational field

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#### 3.1 Numerical series

- 3.1.1 Definition, sum of series, convergence and divergence of a numerical series
- 3.1.2 The ration test (CAUCHY)
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3.1.3.2 Test of comparison with the series  $\sum_{n=1}^{\infty} \left( \frac{1}{n} \right)^{\alpha}$  (RIEMAN test)

- 3.1.4 Absolutely convergence of series
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- 3.1.6 Alternating numerical series, test of LECHNIZ and De DIRICHLET
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  - 3.2.2 ABED'S theorem and segment of convergence
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#### 4.1 First order differential equation

- 4.1.1 Homogeneous equation
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- 4.2 Differential equations of higher order
  - 4.2.1 Linear homogeneous equations, properties of solutions
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## PROBABILITIES

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