

**I-** Reduce the following to simplest possible form:

1.  $5^2 - 3^2 \times 2^2$

2.  $2 \times (3 - 2^2)^3$

3.  $(2^3 \times 3^5)^0$

4.  $(25 - 4^2) \times 9^3$

5.  $(2^3 - 3^5)^0$

6.  $\frac{8^5 - 6 \times 2^{12}}{2^3 \times 4^5}$

**II-** Write the following in the form of prime bases (as fractions with lowest terms):

a.  $(25^{-1})^3 \times 125^2 \times (5^{-5})^{-2}$

b.  $(6 \times 3^2)^3 \times (12 - 2^2)^4$

c.  $(-3^{-2})^{-1} \times (-27^2)^5 \times 81$

d.  $(15^2 \times 25^3)^4 \div 27^2$

**III-** Compare:

a.  $(-3^{12})$                        $(-3^3)$

b.  $(9^3)$                                $(3^6)$

c.  $(-4)^2$                                $(-4)^5$

d.  $(0)^5$                                $(5)^0$

**IV-** Simplify the following expressions:

a.  $-x^{-3} \times (-x^2) \times (-x^3)^2$

b.  $\frac{25x^2 \times (12y^5)^3}{(15x^0)^3 \times (8y^2)^3}$

c.  $\frac{6c}{15b} \times \frac{2ba^2}{3c^2} \div \frac{4a}{9bc}$

d.  $4^x \times 8^{-2x} \times 2^{3x+1}$

**V-** Find  $x$  and  $y$  :

a.  $4^2 \times 2^{x+1} \times 2^{-3} = 2^8$

b.  $6^2 \times 2^{3x} \times 3^{2y-1} = 12^5$

c.  $3^4 \times 9^{2x-1} \times 27^x = 81^3$

d.  $\frac{(2^3 \times 4^y)}{2^{y-1}} = 8^5$

**VI-** Write the following in the form of power of 10, then in decimal form:

a.  $23 \times (10000)^{-1}$

b.  $0.0021 \times 100$

c.  $\frac{1}{4} \times 10^5 \times (0.2 \times 10^{-1})^3$

d.  $10^3 + 10^{-2}$

**VII-** Consider the two numbers  $x = -\frac{1}{3} \times 10^{-2}$  &  $y = -6 \times 10^3$ .

Determine: **a-**  $xy$ .

**b-**  $\frac{2x}{y}$ .

**c-**  $\frac{x^2}{y}$ .

**VIII-** Write in scientific notation:

a.  $\frac{2 \times 10^3 - 2 \times 10^2}{22 \times 10^2}$

b.  $10^{-1} + 10^{-3}$

c.  $325 \times 10^{-7}$

d.  $0.00125 \times 10^6$

**IX-** Given  $C = \frac{8^{20} + 4^{10}}{8^4 + 4^{26}}$

- 1) Verify that  $C=2^8$ .
- 2) Write  $C$  in a scientific notation form.
- 3) Frame  $C$  between two consecutive powers of 10.

**X-** Pick up the only right answer, justifying yourself.

No.	Problem	Expected answer		
		A	B	C
1.	$5 \times 10^{-3} =$	$50^{-3}$	0.005	-150
2.	$10^3 \times \left(-\frac{5}{2}\right)^{-2} \times \frac{5^{-1}}{2^{+3}}$	4	0	10
3.	$\frac{x^{-2}}{y^{-2}} \div \frac{y^{-1}}{x^{-1}}$	$(xy)^{-3}$	$\left(\frac{x}{y}\right)^3$	$\left(\frac{y}{x}\right)^3$
4.	$2^3 + 2^{-3}$	0	$\frac{65}{8}$	$2^0$
5.	$\left. \begin{array}{l} \text{If } r = 11^{27} - 11^{25} \\ \text{and } n = 11^{25} - 11^{24} \end{array} \right\}, \text{ then}$	$\frac{r}{n} = 110$	$\frac{r}{n} = 132$	$\frac{r}{n} = 121$
6.	If $n$ is a natural & $n \neq 0$ then $[(-45)^n]^2 \times [(-7.5)^{2n+1}]^3$ is	Positive	Negative	We cannot tell unless solved

**XI-** Justify that the numerical expressions below are equivalent:

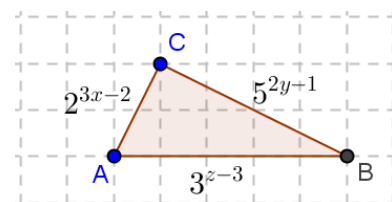
$$R = \left(\frac{3}{4}\right)^2 - \frac{1}{2} \quad \text{and} \quad N = \left(\frac{3}{4} - \frac{1}{2}\right)^2$$

**XII-** Consider the numbers:  $B = \frac{-81 \times 10^5 \times (5 \times 10^{-3})^2}{15^3 \times 10^{-2}}$        $C = 0.001125$

- a. Simplify  $B$ , and then write it in scientific notation.
- b. Write  $C$  in the form of  $d \times 10^n$  where  $d$  is between 1 & 9 and  $n$  is an integer.

**XIII-** Assume that the adjacent figure is a right triangular piece of land.

- a. Find the numerical values of  $x$  &  $y$  so that its area is  $10^3 m^2$ .
- b. To fence this piece of land we used 222m of wires. Deduce the measure of the side  $[AB]$ .
- c. Based on your calculation. Is the given piece of land right at  $C$ ? Give a simple explanation.



**XIV-** Answer by true or false and justify your answer.

- 1)  $A = \frac{3^8 - 9^3}{9^2 + 3^5}$  is a natural number.
- 2) If  $n$  is a non-zero natural number, then the sign of:  $E = -[(-5)^{n+1}]^2 \times [(-7)^{2n+1}]^3$  is negative.

**XV-** Let  $A, B, C$  and  $D$  are four points in the plane such that:

$$AB = \frac{(-7.2)^3 \times (4.8)^2 \times 27^2}{(-24)^2 \times (-3.6)^5 \times 9} \quad ; \quad BC = \frac{2}{3} + \frac{4}{5} \div \left(1 + \frac{3}{5}\right) + \frac{5}{6} \quad ; \quad AC = \frac{49^4 + 5 \times 7^9}{7^8 \times 9}$$

- 1) a) Show that  $AB = 2$ .  
 b) Reduce  $BC$ .  
 c) Verify that:  $AC = AB + BC$ .
- 2) a) What can you deduce about the points  $A, B$  and  $C$ ?  
 b) Deduce the relative position of the point  $B$  with respect to  $[AC]$ . (Draw a figure)
- 3) Consider the numbers:  $AD = 5^2 \times (2^2 + 1)^2 \div 5^3$  and  $DC = GCD(65; 75)$ 
  - a. Write  $AD$  in the form of a power of 5.
  - b. Calculate  $DC$ .
  - c. What is the relative positions of:
    - i. The point  $D$  with respect to the points  $A$  and  $C$ .
    - ii. The straight line  $(DB)$  represent to the segment  $[AC]$ ? Justify.

<b>Mastering problems</b>		
<i>Chapter</i>	<i>Exercises</i>	<i>Pages</i>
CH-: Powers	1, 2, 4, 6, 10, 11, 13, 18 & 19	12 → 19
	3 & 4	240
	5 & 7	241