$f2x + y = 8\dots(a)$ Given the system:  $\begin{cases} 3x - 4y = 1 \dots (b) \end{cases}$ *I*-|mx + (m+1)y = 12....(c)

- *a*. Solve the system formed by the two equations a & b.
- b. Calculate the value of m such that the ordered pair that verifies the 1<sup>st</sup> two equations is a solution of equation (*c*).

II-Solve the following systems:

a) 
$$\begin{cases} 5x + 2y = 2x + 1\\ 2x - 3y = 3x + 2 \end{cases}$$
, b) 
$$\begin{cases} \frac{2}{2x - 1} + \frac{3}{z + 2} = 10\\ \frac{5}{2x - 1} - \frac{1}{z + 2} = 8 \end{cases}$$
; c) 
$$\begin{cases} 3(a^2 - 1) + 2(b^2 + 1) = 58\\ 2(a^2 - 1) - 5(b^2 + 1) = -69 \end{cases}$$

$$d) \begin{cases} \frac{2p}{3} - \frac{4q}{5} = \frac{2+q}{5}; \\ 2p = 3q \end{cases} \qquad e) \begin{cases} 2z - 5w = -1 \\ az - (a+1)w = 2a - 3; f \end{cases} \begin{cases} (4n - r)^2 + (4n - r)(n + 2r) = 54 \\ 5n + r = 6 \end{cases}$$
$$g) \begin{cases} x + 3y = 13 \\ xy = 12 \end{cases}; \qquad h) \begin{cases} y = 3x + 1 \\ y = 6x^2 - 2x \end{cases}; \qquad i) \begin{cases} x^2 - 3y = 16 \\ x - y = 2 \end{cases}.$$

- III- A scarf and a jacket will cost Mariam 72 \$. The shop offers a 30% sale on the price of the jacket and 10% tax is added to that of the scarf so that the total price will be 66.\$.
  - a. Write the expressions that describes the prices after the increase and the decrease.
  - b. Determine the initial prices of both items.
- Find the real numbers A and B such that the graphs of the two equations Ax+2y = 2 and IV-2x+By = 10 intersect at the point (2;-2).
- Find the value of a, such that the lines:  $(d_1)$ : y = 2x + 7;  $(d_2)$ : y = -x + 1 and  $(d_3)$ : y = ax 1Vintersect at the same point.
- *VI* Prove the following equality:  $\frac{1}{(x-1)} + \frac{1}{(x-1)(x-2)} + \frac{1}{(x-2)(x-3)} = \frac{1}{(x-3)}$ .

Then deduce the values of the three positive numbers: a, b & c such that:  $\frac{1}{a} + \frac{1}{b} + \frac{1}{c} = \frac{1}{7}$ .

- VII- The hypotenuse of a right triangle is greater than one of the other two arms by 10cm and the third arm is 70cm.
  - a. Translate the above text into a system of two equations with two unknowns.
  - *b*. Solve the formed system to find the length of the hypotenuse.

*VIII*-The perimeter of the rectangle *ABCD* is 22*cm* and that of the triangle is12*cm*.



- a. Prove that the expressions of the peri
- b. meters of the two given geometric figures can be translated into the following system of two equations.

2y + 3x = 103x + 5y = 16

- c. Solve in  $\Re$  the formed system.
- d. Find the length of the sides of EFG. Deduce its nature.

*a*) Solve the system: 
$$\begin{cases} \frac{A}{9} = \frac{B}{7} \\ A - 3B \end{cases}$$

= -1

b) The sum of two fractions is eight times their difference; and three times the smaller exceeds the larger by 1. Find the terms of this fraction.

Consider the following system: *X*-

$$\begin{cases} x+y-35=0\\ 260-8x=7y \end{cases}$$

IX-

- a. Find the couple (x; y) that verifies the above system.
- b. The fuel and water reserves in a certain power plant is 35 000 liters. After it consumes 20% of the fuel reserve and 30% of the water reserve, the level of the tanks decreases to 26 000 liters. Find the original amount of fuel and water reserves.
- In the following figure x is expressed in *cm*. Use the figure given below to calculate x if *RI* XIis a median relative to hypotenuse of triangle RNK.



- XII- At an electronics shop, Rajaa bought memory card and 3 CD's for 30\$. From the same shop Fouad bought 2 cards and one CD paid 21\$. For a specific reason Khalil took 8 cards and 10 CD's. How much did Khalil pay?
- *XIII*-Use the following table of proportionality to compute *x* & *y*:

2x - 3	3	y – 5
<i>y</i> + 1	4	<i>x</i> + 2

XIV- A merchant sells mixtures of coffee made up of two types.

*Mixture-A*: Costs 15\$ per kilo and it is made up of 60% Colombian coffee and 40% of Brazilian coffee.

*Mixture-B*: Costs 13.5\$ per kilo and it is made up of 40% Colombian coffee and 60% of Brazilian coffee.

A customer enters the shop and wants to make up his own mixture, which is composed of 30% Brazilian coffee and 70% Colombian coffee.

Assist the merchant to price the formed kilo.

- *XV* Translate each of the following word problems into mathematical equations without solving them:
  - a. The difference between 55 and four times a number is equal to fifteen.
  - *b*. Nada is 48 years old and her daughter is 6 years old. In how many years will the age of Nada be three times her daughter's?
  - *c*. The age of a father is 5 years more than four times the age of his son. After ten years, his age become seven years less than the triple of the age of his son.
  - *d.* Jamal's present age is three-fourths of Sara's present age. In five years, Jamal's age will be four-fifths of Sara's age at that time. What are the present ages of Jamal's and Sara?
  - e. Two numbers have a ratio of  $\frac{3}{4}$ . If the greater is increased by 140, and then the obtained number will be double the smaller.
  - f. The value of a fraction is  $\frac{1}{2}$ , if its numerator is reduced by 1 and the denominator is increased by 2. We get the same value if numerator is raised by 1 and the denominator is doubled.
  - g. Find a two digit number that is three times the sum of its digits, knowing that if we add 45 to this number then its digits will be reversed.
- *XVI* Sara bought a number of copybooks at Malik's for 150\$. If each copybook had been 5\$ more, then 5 fewer could have been purchased. Find the price of each copybook. (*Hint*: let *x* be the number of copybooks and \$y be the cost of each).



*XVII*- In the below figure: AB = 2cm, AC = 6cm & AG = y. Where  $P_{ADFG} = 6cm$ . Find x & y.



XVIII-In the figure below, the measures are given in cm. Compute x & y.

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