

I- Answer the following questions:

1- Given $\tan \alpha = -2$ and $\frac{\pi}{2} < \alpha < \pi$. Calculate $\cos \alpha$ & $\sin \alpha$ then deduce the value of

$$E = \cos\left(\frac{5\pi}{2} + \alpha\right) \times \sin\left(\frac{-7\pi}{2} + \alpha\right).$$

2- Given $\tan x = \frac{3}{4}$, where $\pi < x < \frac{3\pi}{2}$. Calculate $\cot x, \cos x$ & $\sin x$, then deduce the value of

$$M = \cot(5\pi - x) - 3\sin\left(\frac{3\pi}{2} - x\right) + 2\cos\left(-\frac{\pi}{2} + x\right).$$

3- Given $\cos \alpha = -\frac{3}{5}$ and $\alpha \in]\pi, \frac{3\pi}{2}[$. Calculate $\cos^2 \alpha + 3\sin \alpha - 2\cot \alpha$.

4- Given $\sin x = -\frac{4}{5}$ and $-\frac{\pi}{2} < x < \frac{\pi}{2}$. Calculate $5\cos^2 x + \cos(3\pi + x) + 4\tan x$.

5- Given $5\sin^2 \alpha + \cos^2 \alpha = 2$ and $0 < \alpha < \frac{\pi}{2}$. Calculate $E = \sin \alpha + \cos \alpha - 3\cot \alpha$.

6- Given $\sin \frac{\pi}{8} = \frac{\sqrt{2-\sqrt{2}}}{2}$

a. Calculate $\cos \frac{\pi}{8}$ and $\tan \frac{\pi}{8}$.

b. Deduce the values of $\cos \frac{7\pi}{8}, \sin \frac{5\pi}{8}$ and $\tan \frac{3\pi}{8}$.

II- 1) x, y, z & t are the angles of a parallelogram $ABCD$.

$$\text{Show that: } \sin^2 x + \sin^2 y + \sin^2 z + \sin^2 t + \sin^2(x + y + z + t) = \frac{4}{1 + \cot^2 x}.$$

2) Let a & b be two arcs such that: $a - b = \frac{\pi}{2}$ and $\frac{\sin a}{\sin b} = \frac{1}{2}$, where $0 < a < \pi$.

Calculate $\sin a, \cos a,$ & $\tan a$.